

# EngrD 2190 – Lecture 27

Concept: Graphical Models for Mass Balances

Context: Operating Lines for Distillation, cont'd.  
The McCabe-Thiele Method.

Defining Question: What is the range of valid  
liquid+vapor mixtures for a distillation  
feed stage?

Read Chapter 5 pp. 423-431.  
Dimensional Analysis & Dynamic Scaling

# Lecture Friday 11/7 is cancelled

Lecture is cancelled to accommodate the distillation lab session.

Although your lab session will not be Friday 11/7 9:05-9:55 a.m.

**The cancelled lecture allows for the lab session  
without increasing the net contact hours.**

Distillation lab sessions will commence Thursday 11/13.

Sign-up for a 50-minute lab session.

Two homework teams per session.

**Submit Homework 7 (due Friday 11/7) by delivering  
to the EngrD 2190 mailbox outside 116 Olin Hall.**

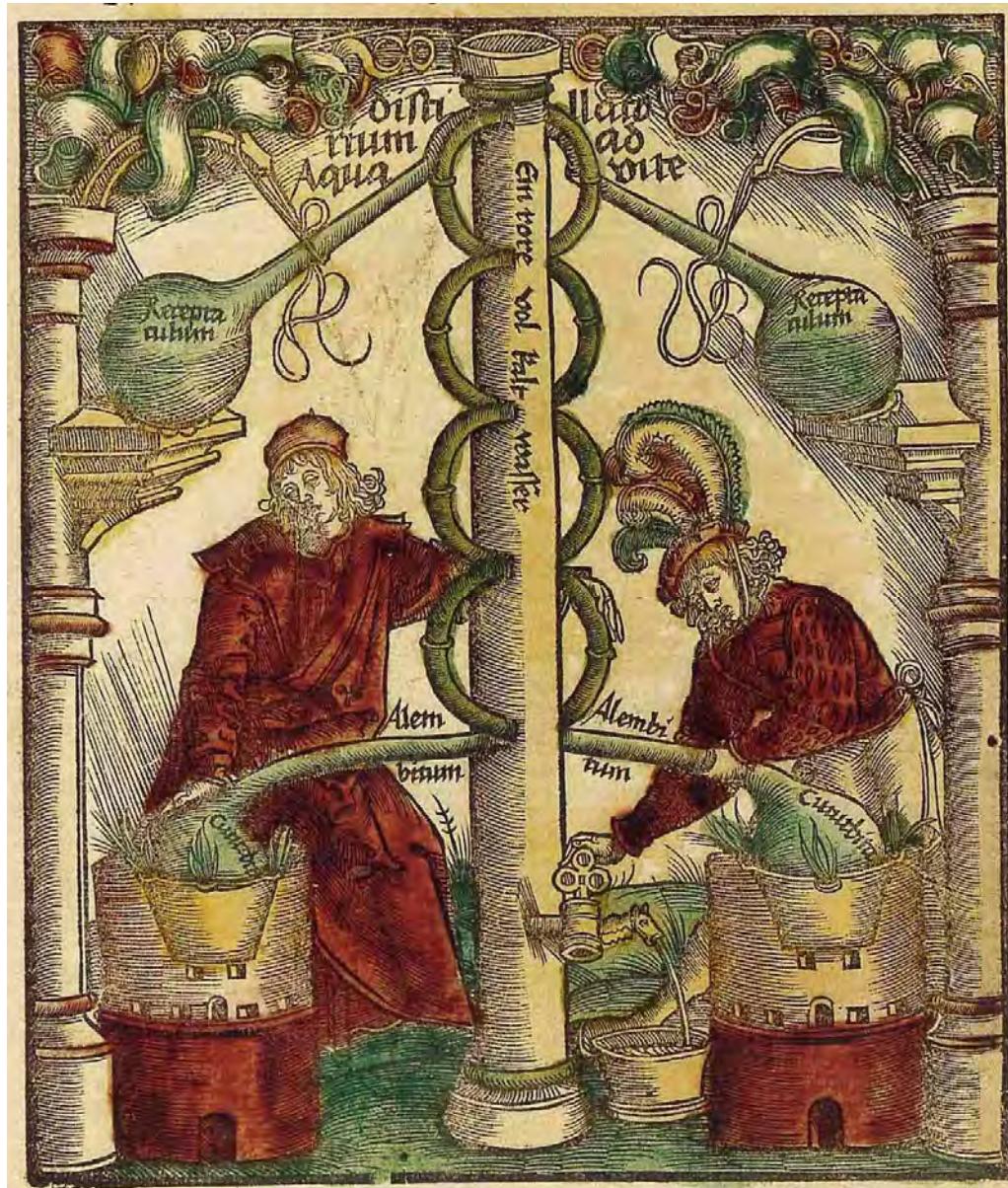
# Homework

- Homework 8 due Friday 11/14.
  - 4.67 & 4.68** analysis of distillation columns.
  - 4.108** design with distillation columns.
  - 4.103** design with ternary diagrams.

Download blank graphs and phase data from EngrD 2190 homepage:

Textbook → Textbook Graphs and Figures →  
Graphs for Chapter 4 Exercises.

*Homework is your chief means of assessing your command of the material.*

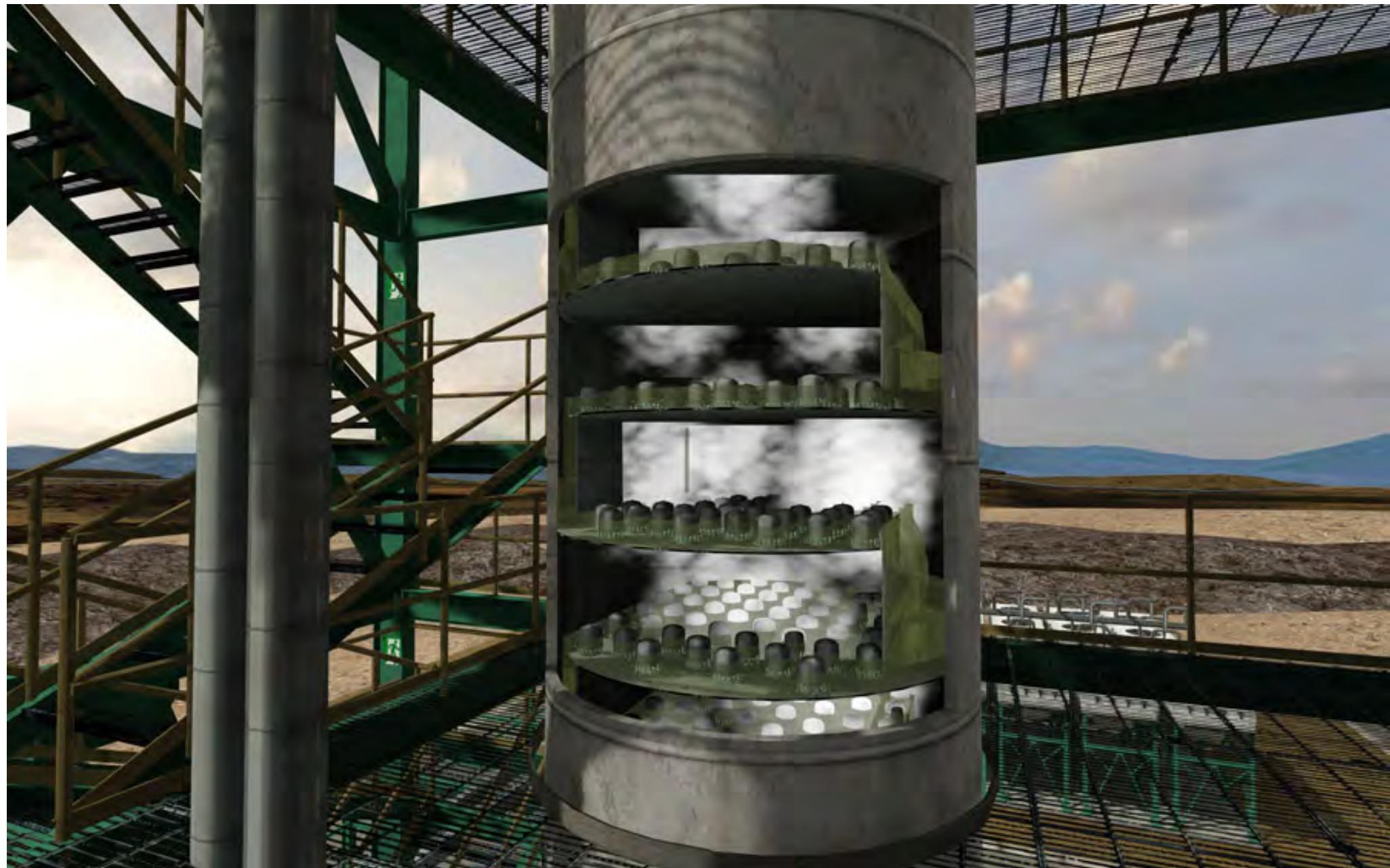


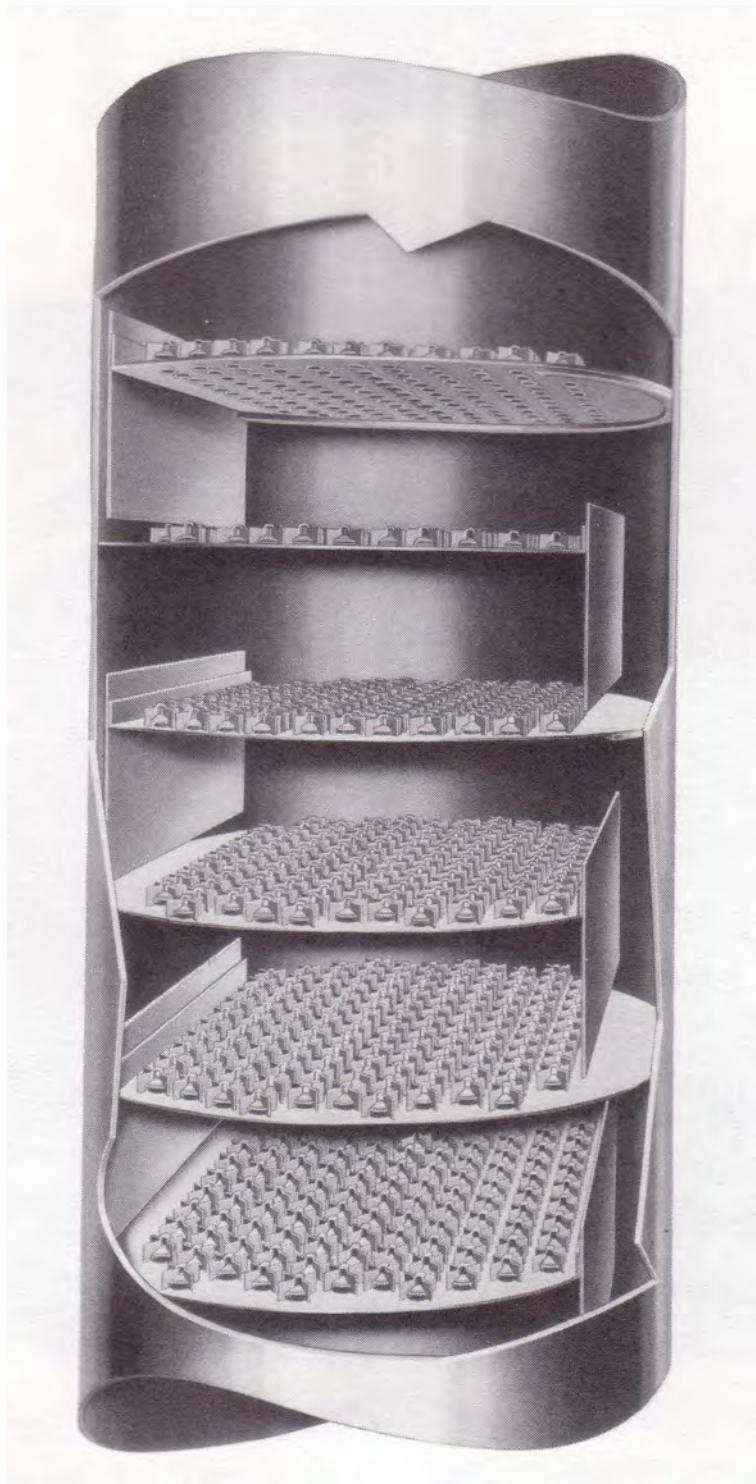
*Liber de arte Distillandi*, by Hieronymus Brunschwig, 1527.

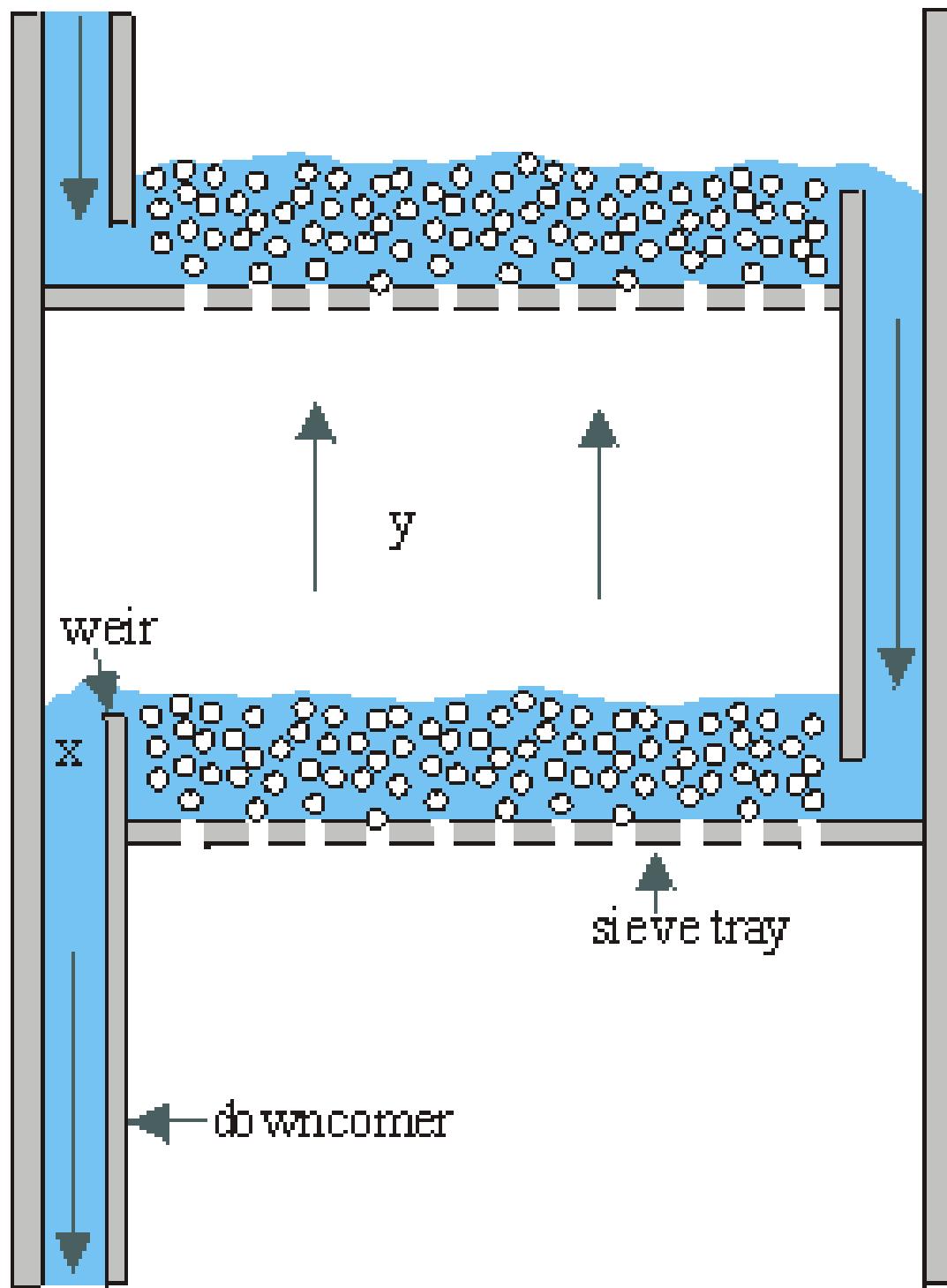


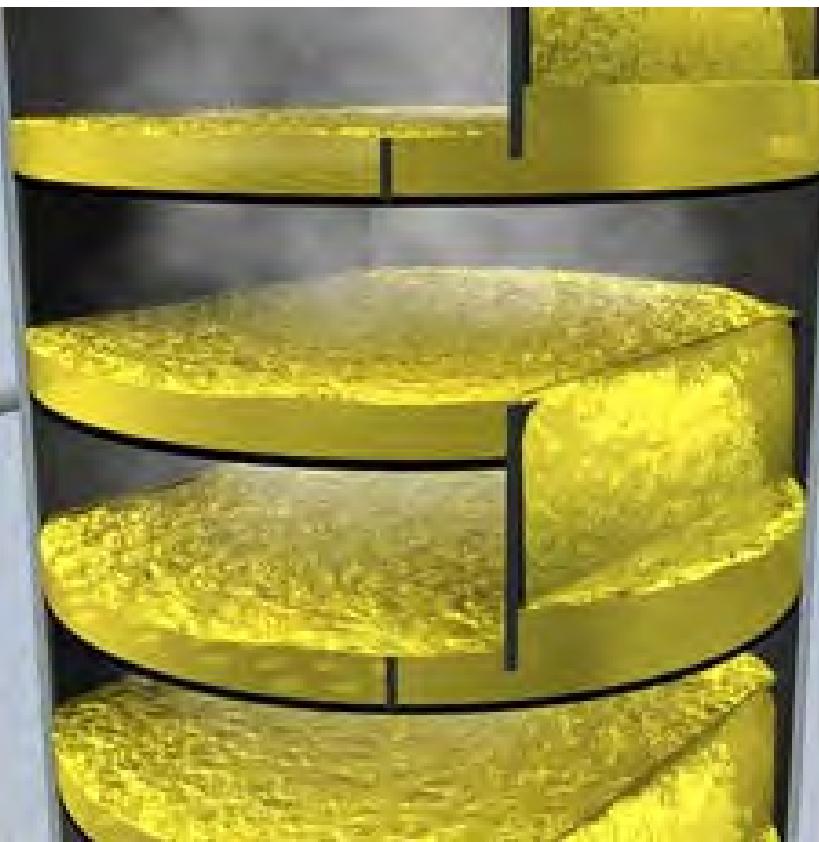


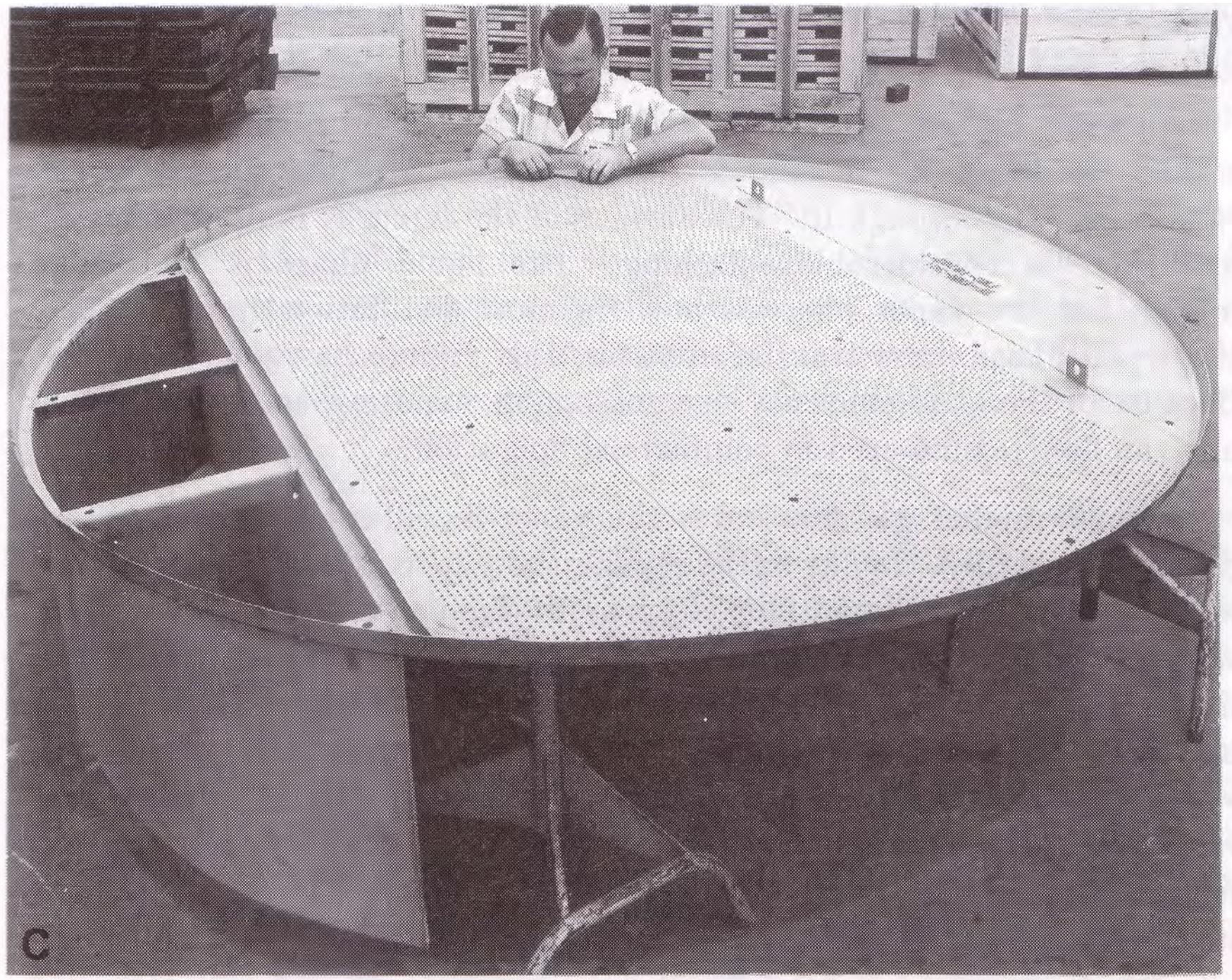




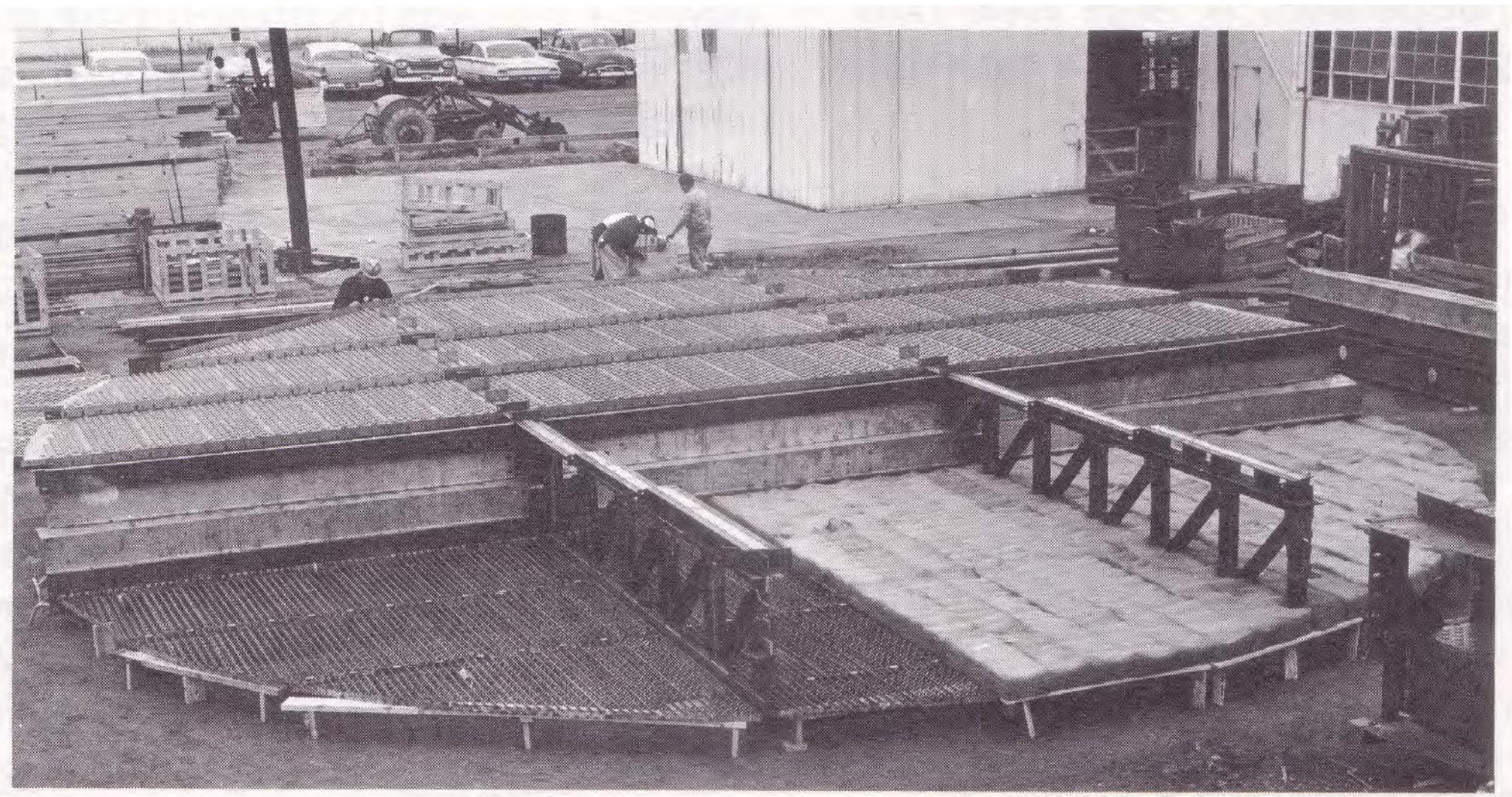








C





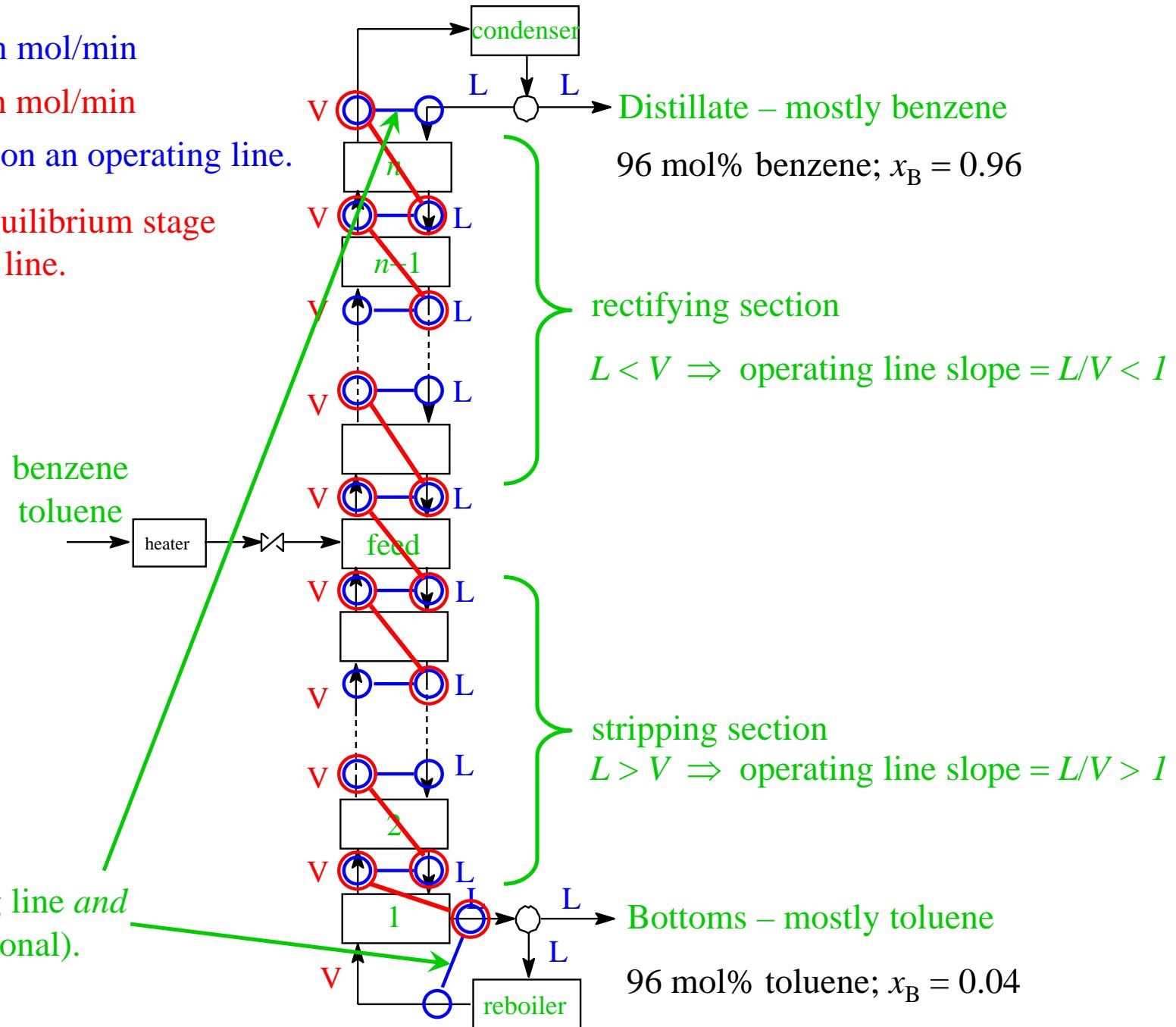
# A Distillation Column

$L$  ≡ liquid flow rate, in mol/min

$V$  ≡ vapor flow rate, in mol/min

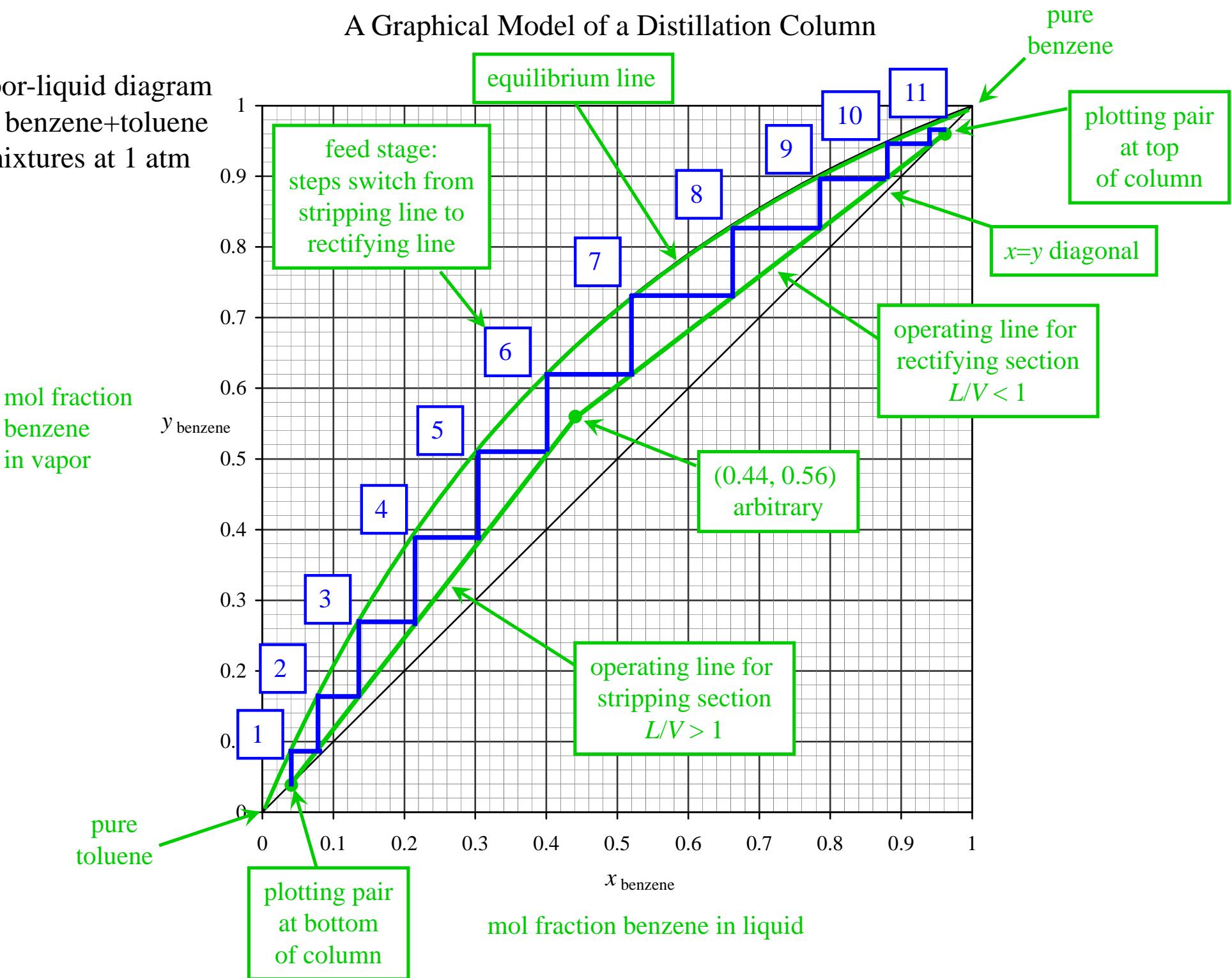
Adjacent  $x$ - $y$  pairs are on an operating line.

$x$ - $y$  pairs leaving an equilibrium stage are on the equilibrium line.



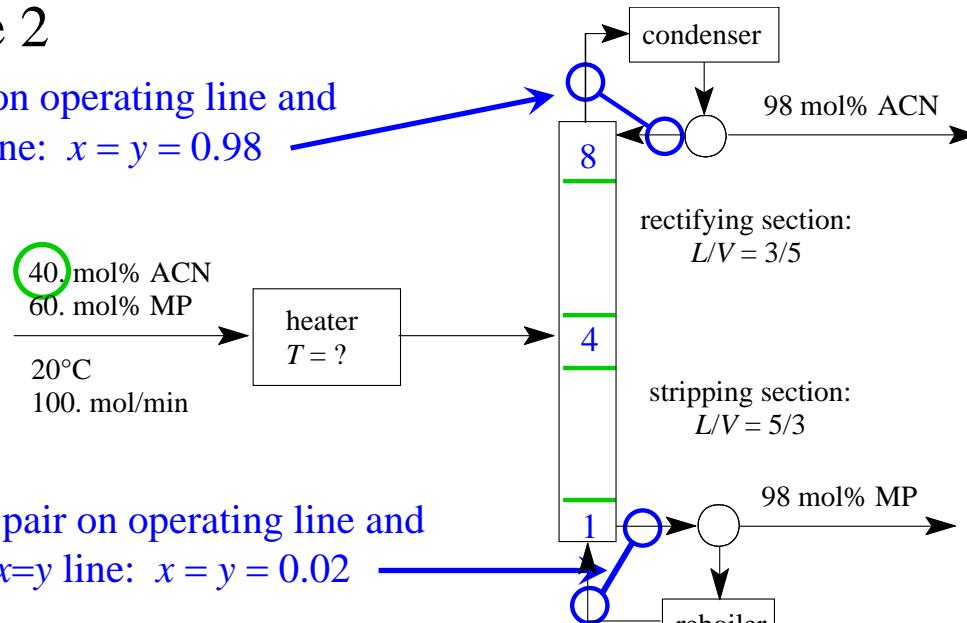
vapor-liquid diagram  
for benzene+toluene  
mixtures at 1 atm

## A Graphical Model of a Distillation Column



## Distillation Example 2

*x-y pair on operating line and on  $x=y$  line:  $x = y = 0.98$*



$$\text{slope} = \frac{\text{rise}}{\text{run}} = \frac{3}{5} \times \frac{0.10}{0.10} = \frac{0.30}{0.50}$$

$$x: 0.98 - 0.50 = 0.48$$

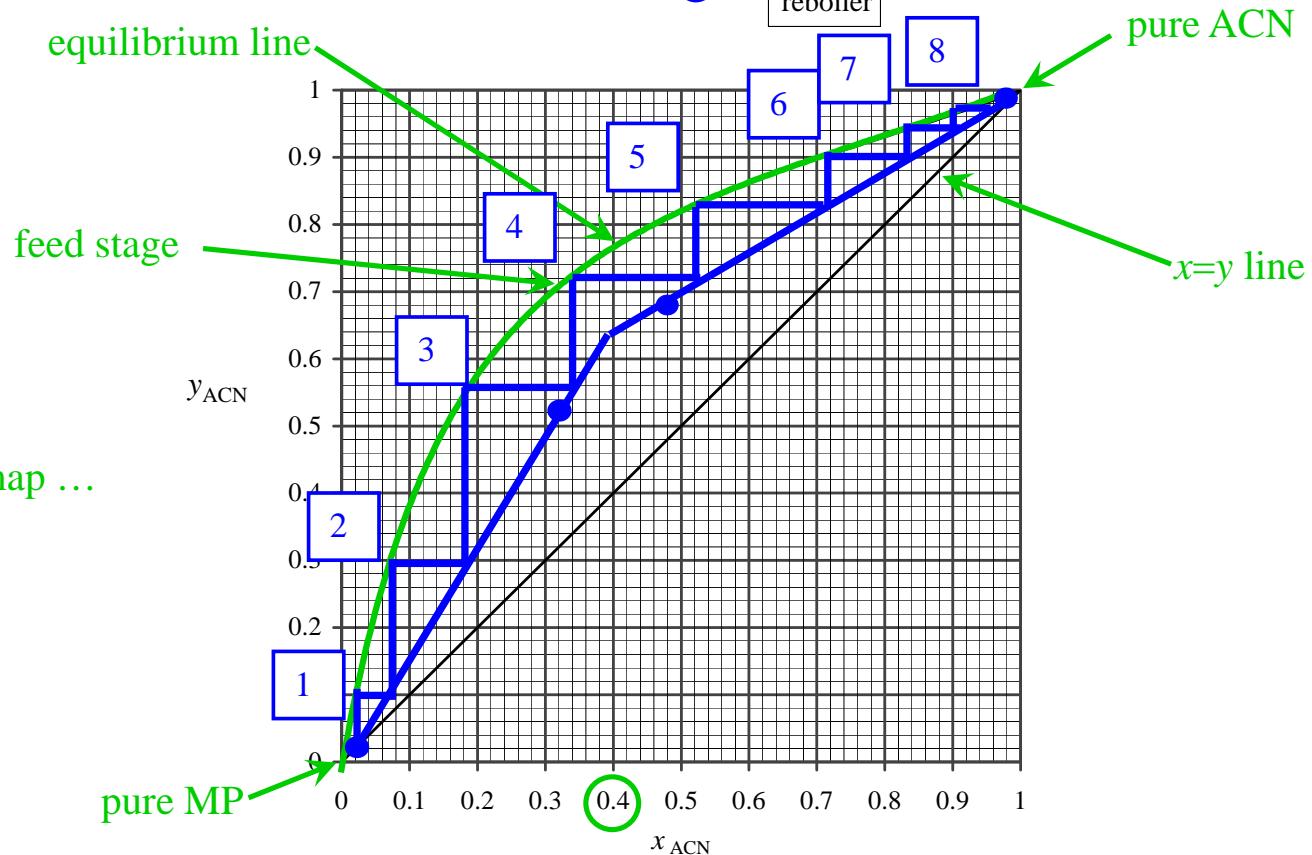
$$y: 0.98 - 0.30 = 0.68$$

$$\text{slope} = \frac{\text{rise}}{\text{run}} = \frac{5}{3} \times \frac{0.10}{0.10} = \frac{0.50}{0.30}$$

$$x: 0.02 + 0.30 = 0.32$$

$$y: 0.02 + 0.50 = 0.52$$

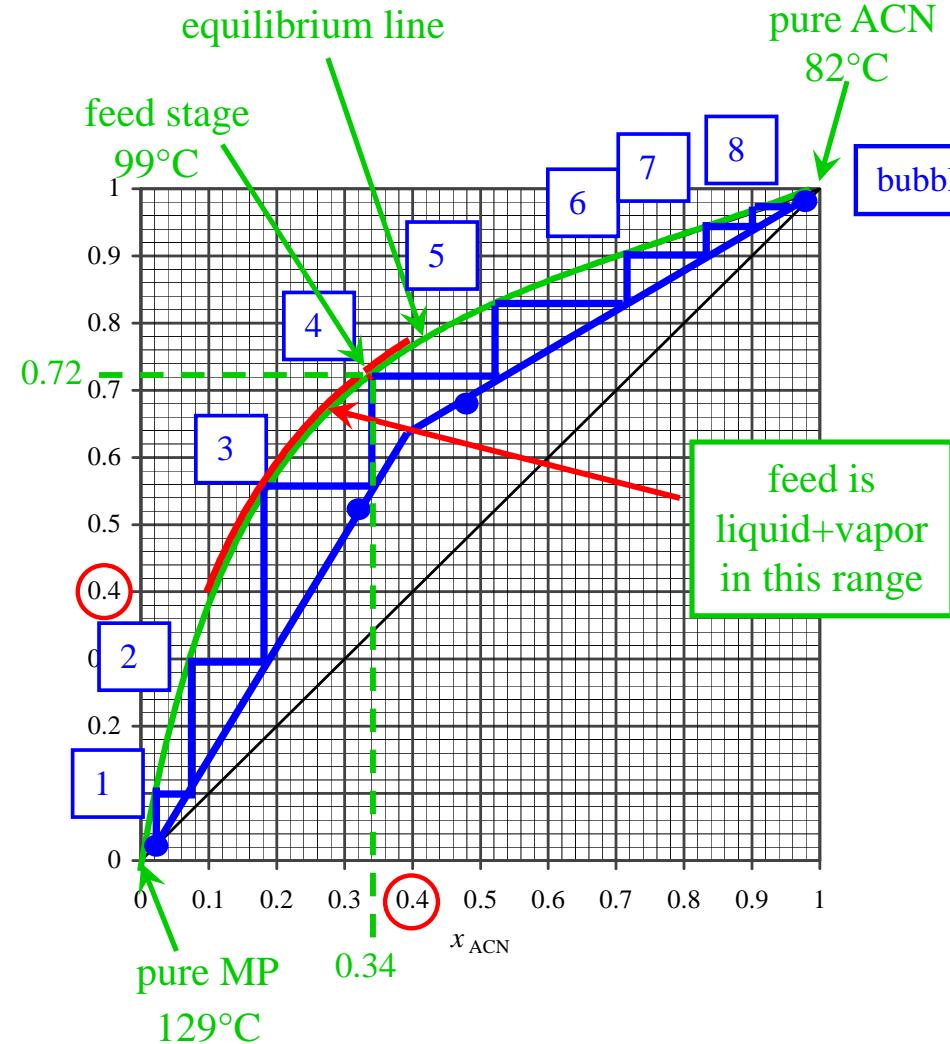
*x-y pair on operating line and on  $x=y$  line:  $x = y = 0.02$*



Temperature of feed?

We need a different map ...

## Distillation Example 2, continued.

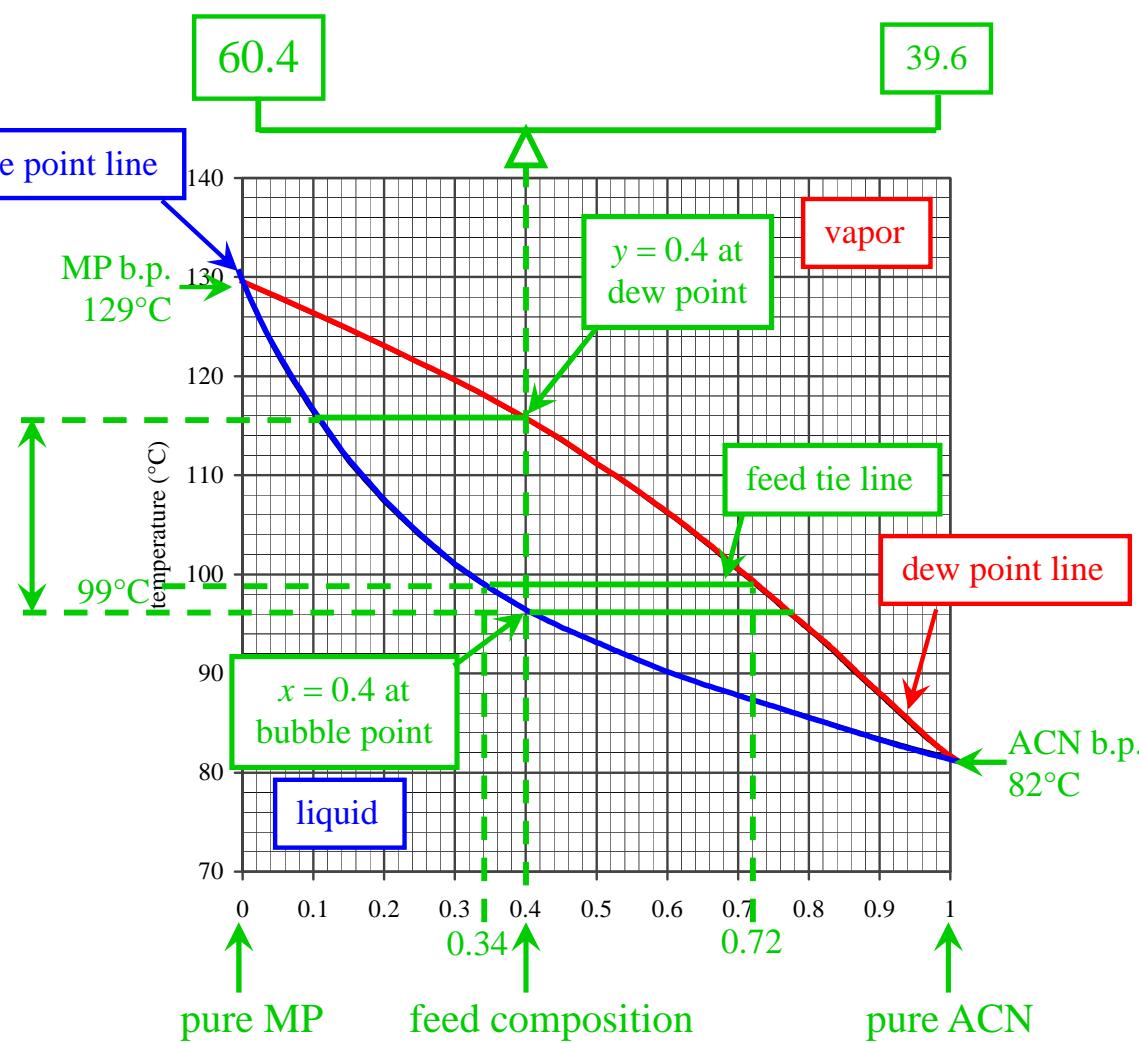


liquid+vapor everywhere

## Equilibrium on one line only

Need two streams to plot a point

## Use operating lines



liquid+vapor in one region only

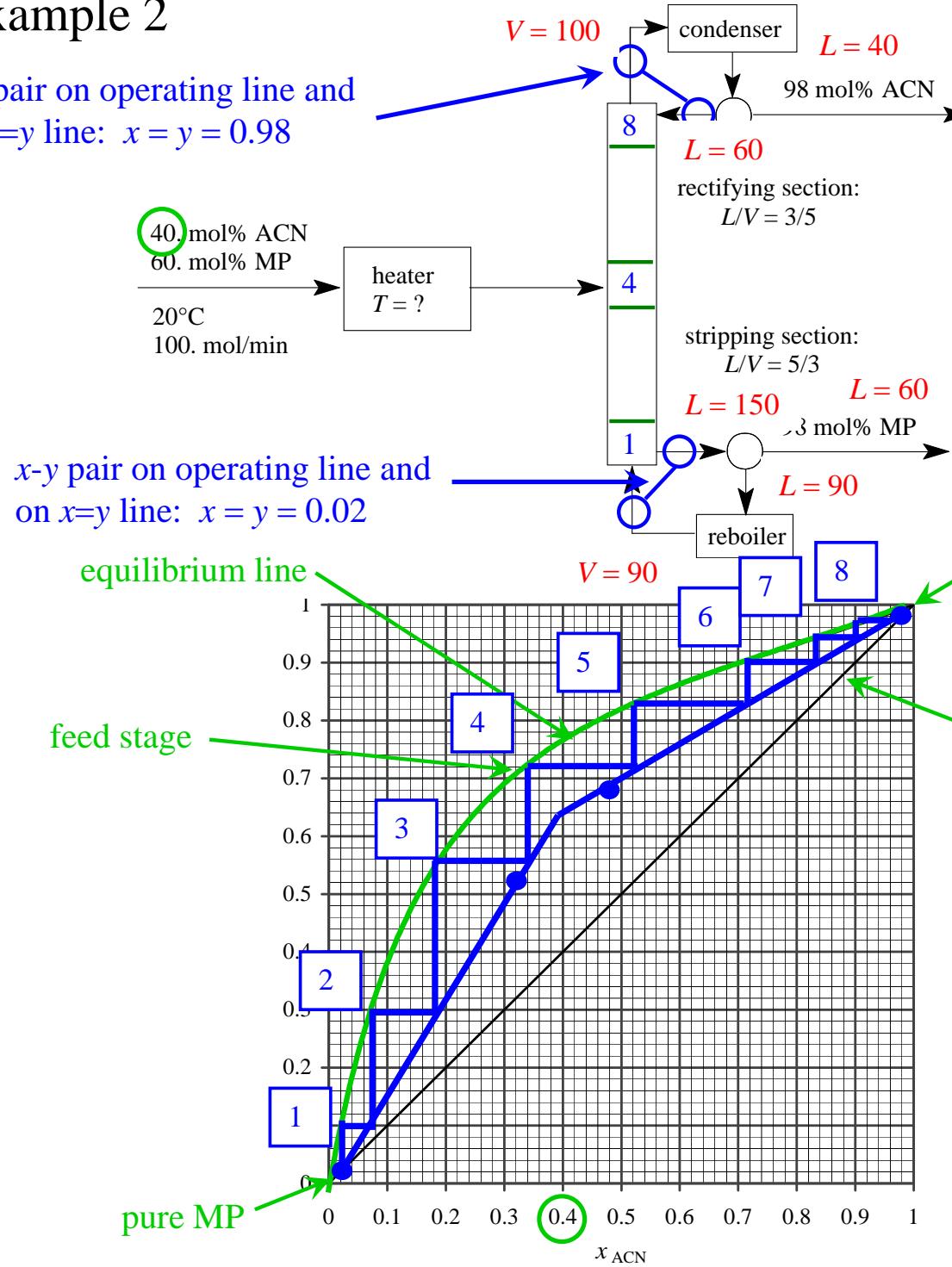
## Equilibrium everywhere

One stream defines a point

## Use tie lines

## Distillation Example 2

$x-y$  pair on operating line and on  $x=y$  line:  $x = y = 0.98$



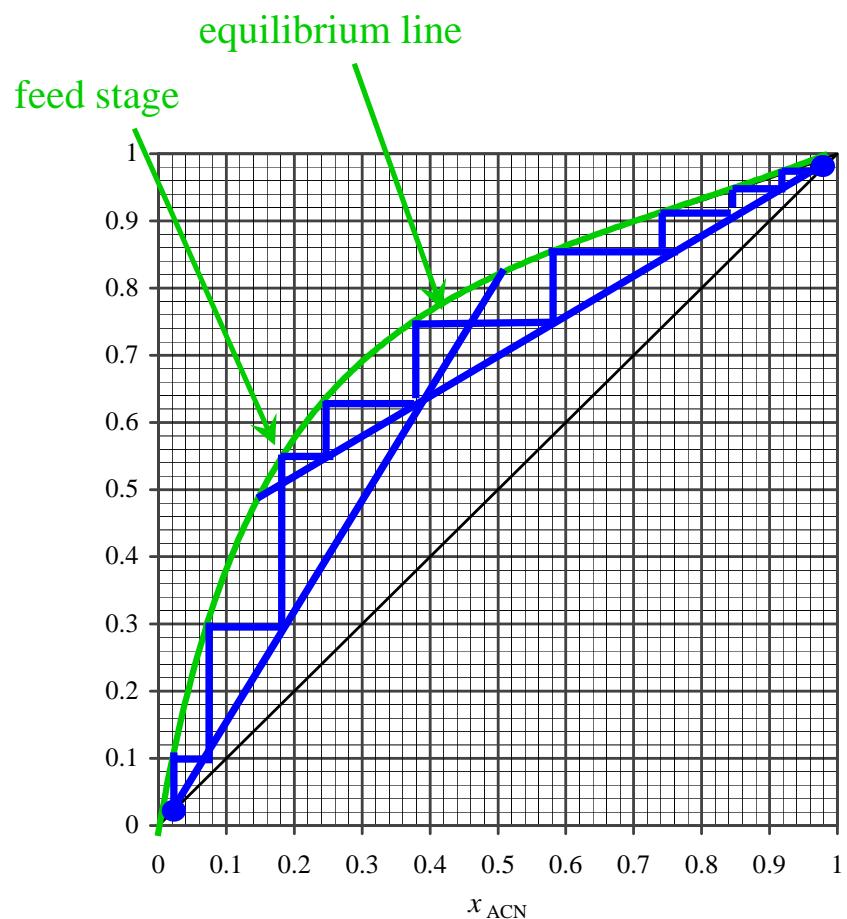
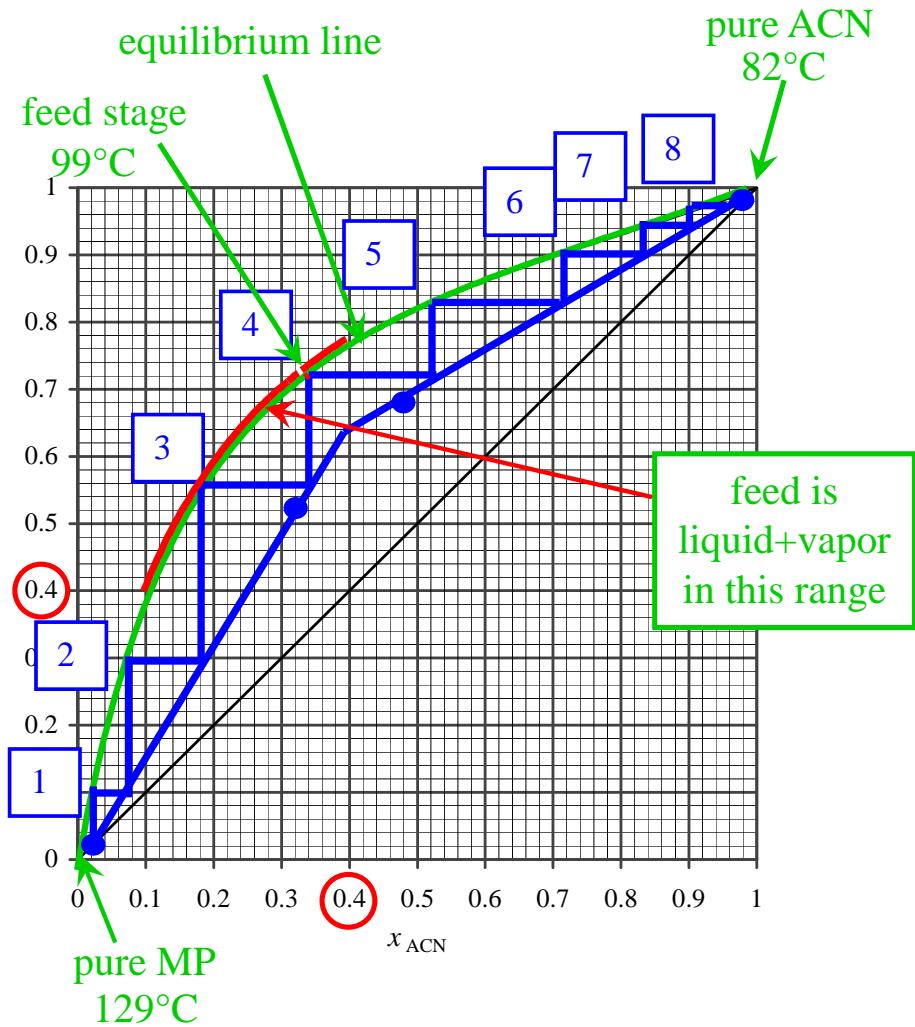
$$\text{slope} = \frac{\text{rise}}{\text{run}} = \frac{3}{5} \times \frac{0.10}{0.10} = \frac{0.30}{0.50}$$

$$x: 0.98 - 0.50 = 0.48$$

$$\text{slope} = \frac{\text{rise}}{\text{run}} = \frac{5}{3} \times \frac{0.10}{0.10} = \frac{0.50}{0.30}$$

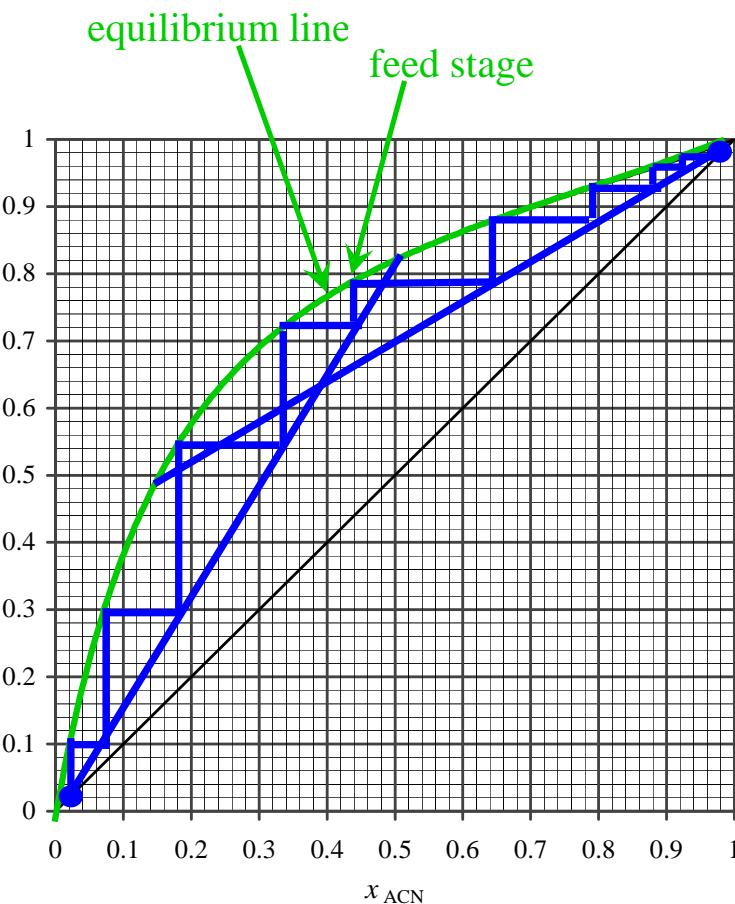
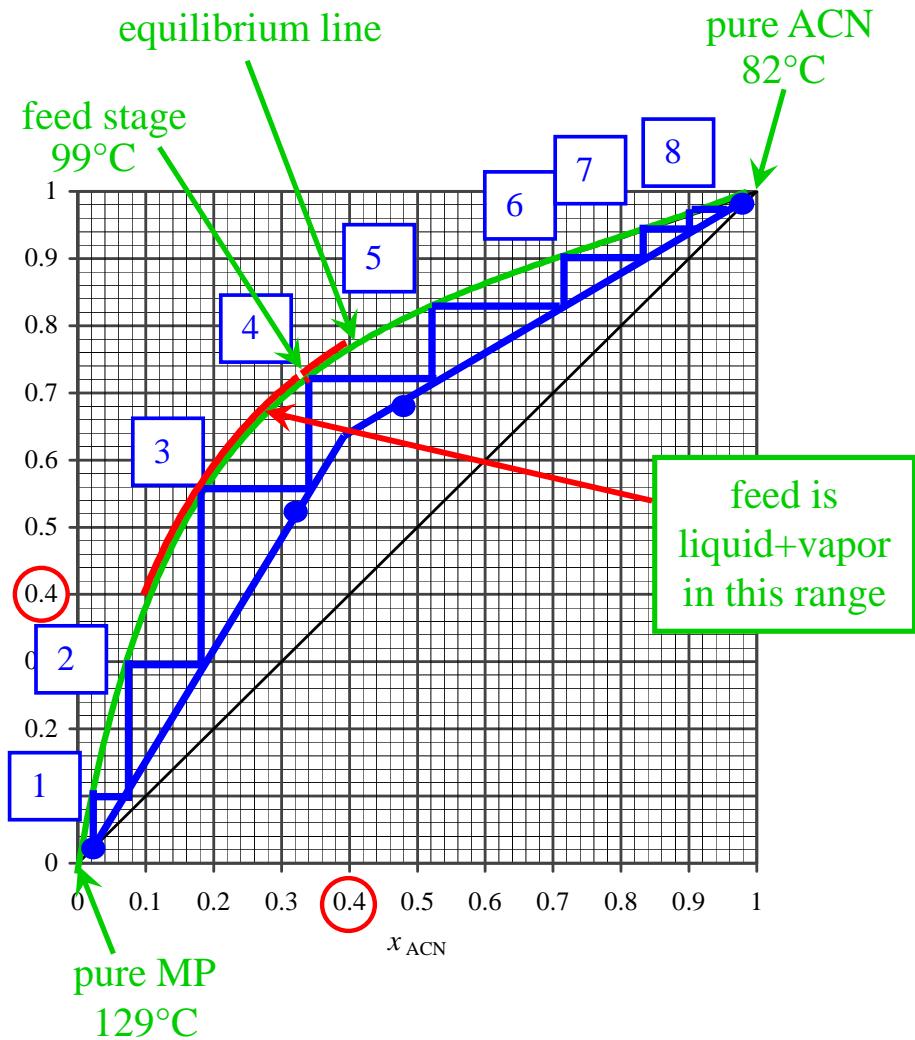
$$x: 0.02 + 0.30 = 0.32$$

## Distillation Example 2, continued.



Same operating lines  
 Valid construction? Valid operation?  
 Valid!

## Distillation Example 2, continued.



Same operating lines  
Valid construction? Valid operation?  
Not Valid!

# Prelim 2 2025 Statistics

Mean:  $90 / 120$  (75%)

Std. Deviation: 20

A - K: Kong (Front of room)

L - Z: Angel (Back of room)

*Solution is posted.*

Problem 1:  $22 \pm 8 / 35$  (62%)

Problem 2:  $18 \pm 3 / 20$  (90%)

Problem 3:  $13 \pm 6 / 20$  (69%)

Problem 4:  $15 \pm 5 / 20$  (77%)

Problem 5:  $20 \pm 7 / 25$  (78%)