

EngrD 2190 – Lecture 27

Concept: Graphical Models for Mass Balances

Context: Operating Lines for Distillation, cont'd.
The McCabe-Thiele Method.

Defining Question: What is the range of valid
liquid+vapor mixtures for a distillation
feed stage?

Read Chapter 5 pp. 423-431.

Dimensional Analysis & Dynamic Scaling

Lecture Friday 11/7 is cancelled

Lecture is cancelled to accommodate the distillation lab session.

Although your lab session will not be Friday 11/7 9:05-9:55 a.m.

**The cancelled lecture allows for the lab session
without increasing the net contact hours.**

Distillation lab sessions will commence Thursday 11/13.

Sign-up for a 50-minute lab session.

Two homework teams per session.

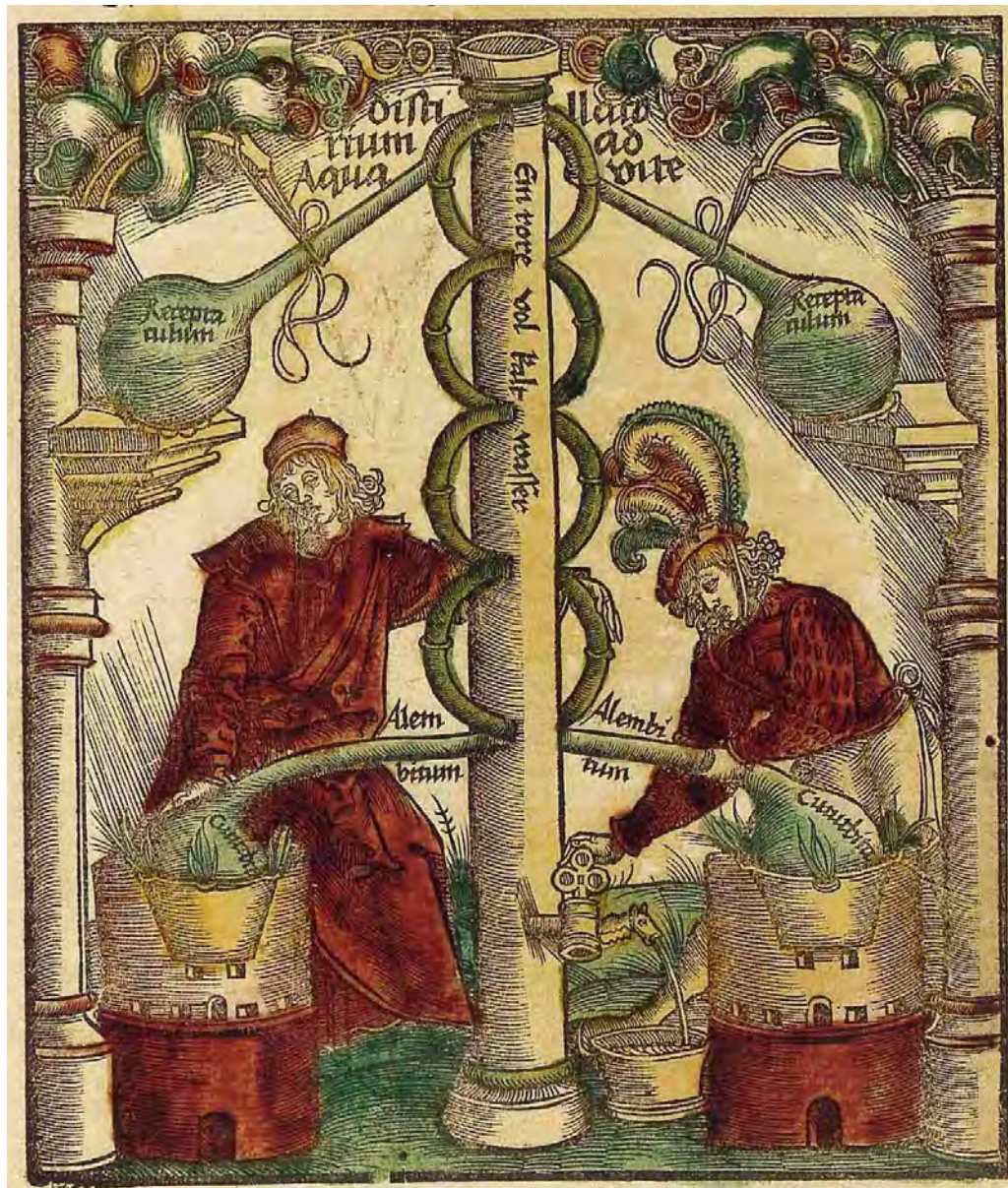
**Submit Homework 7 (due Friday 11/7) by delivering
to the EngrD 2190 mailbox outside 116 Olin Hall.**

Homework

- Homework 8 due Friday 11/14.
 - 4.67 & 4.68** analysis of distillation columns.
 - 4.108** design with distillation columns.
 - 4.103** design with ternary diagrams.

Download blank graphs and phase data from EngrD 2190 homepage:
Textbook → Textbook Graphs and Figures →
Graphs for Chapter 4 Exercises.

Homework is your chief means of assessing your command of the material.

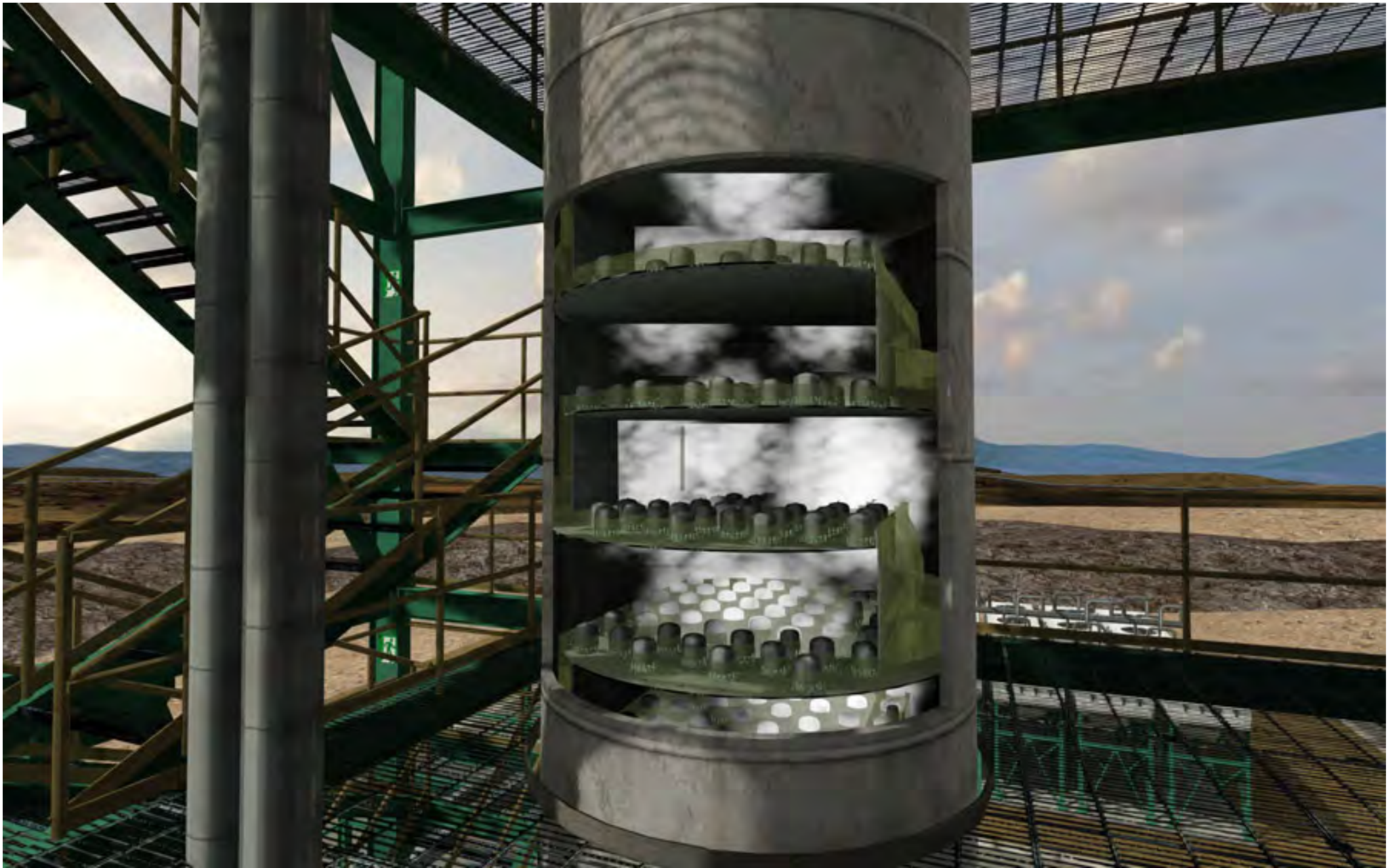


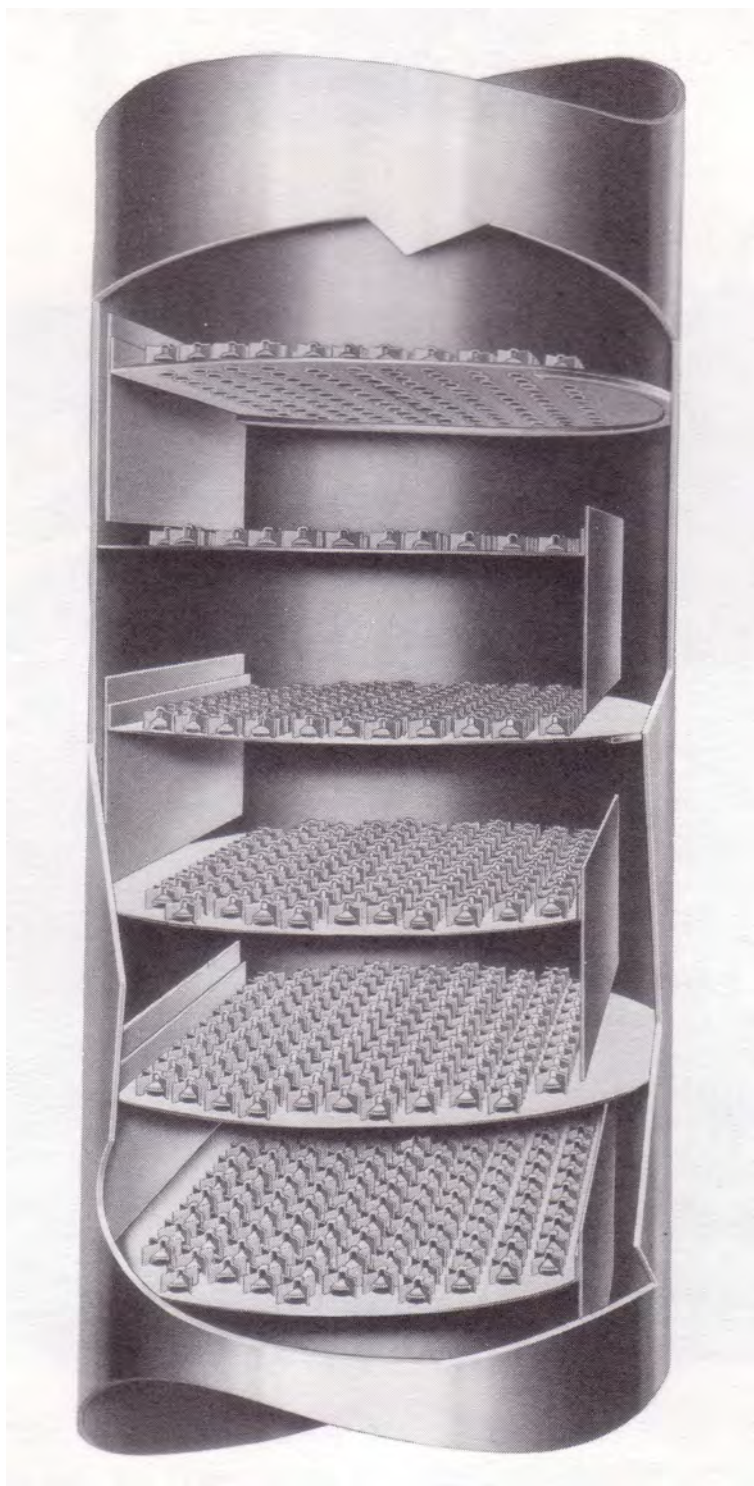
Liber de arte Distillandi, by Hieronymus Brunschwig, 1527.

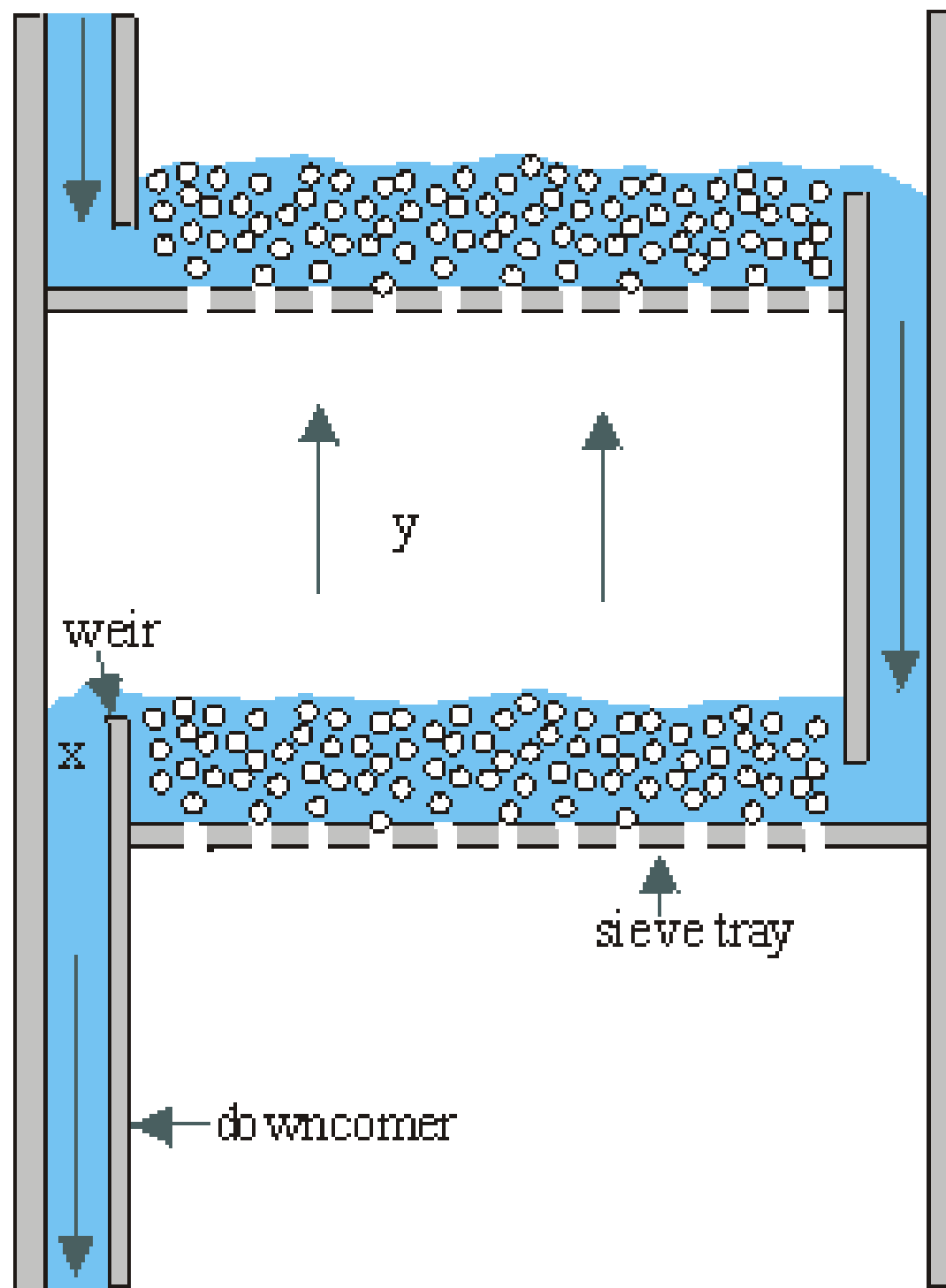


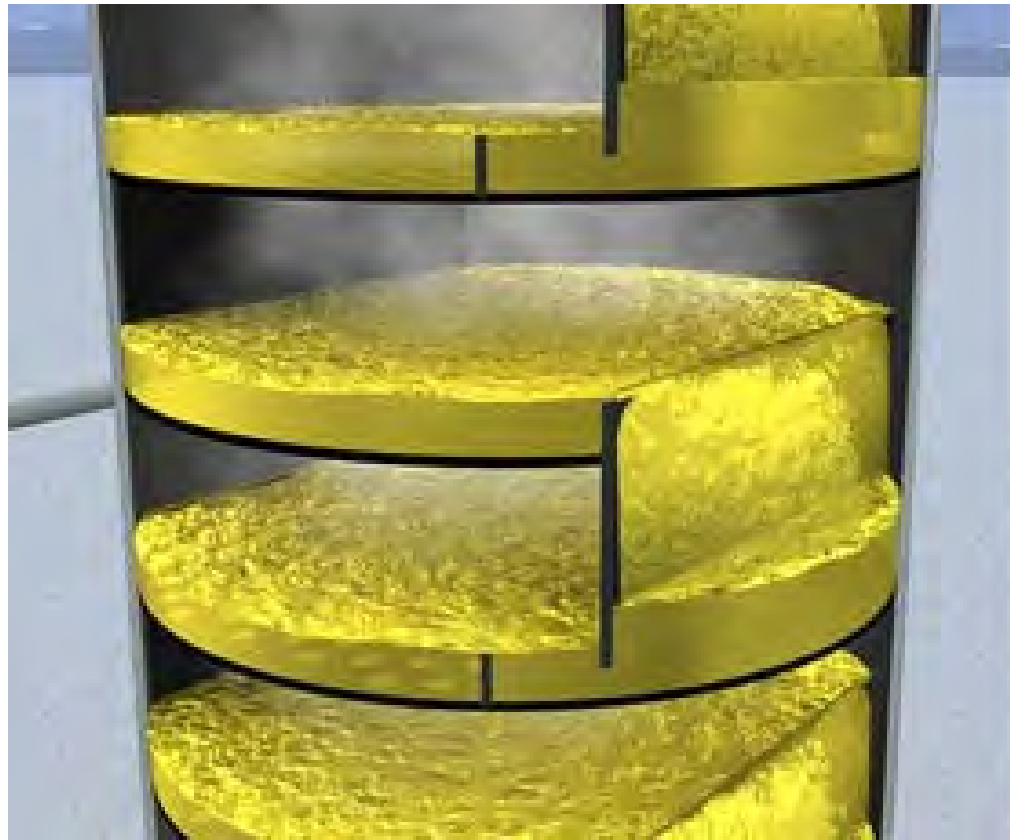






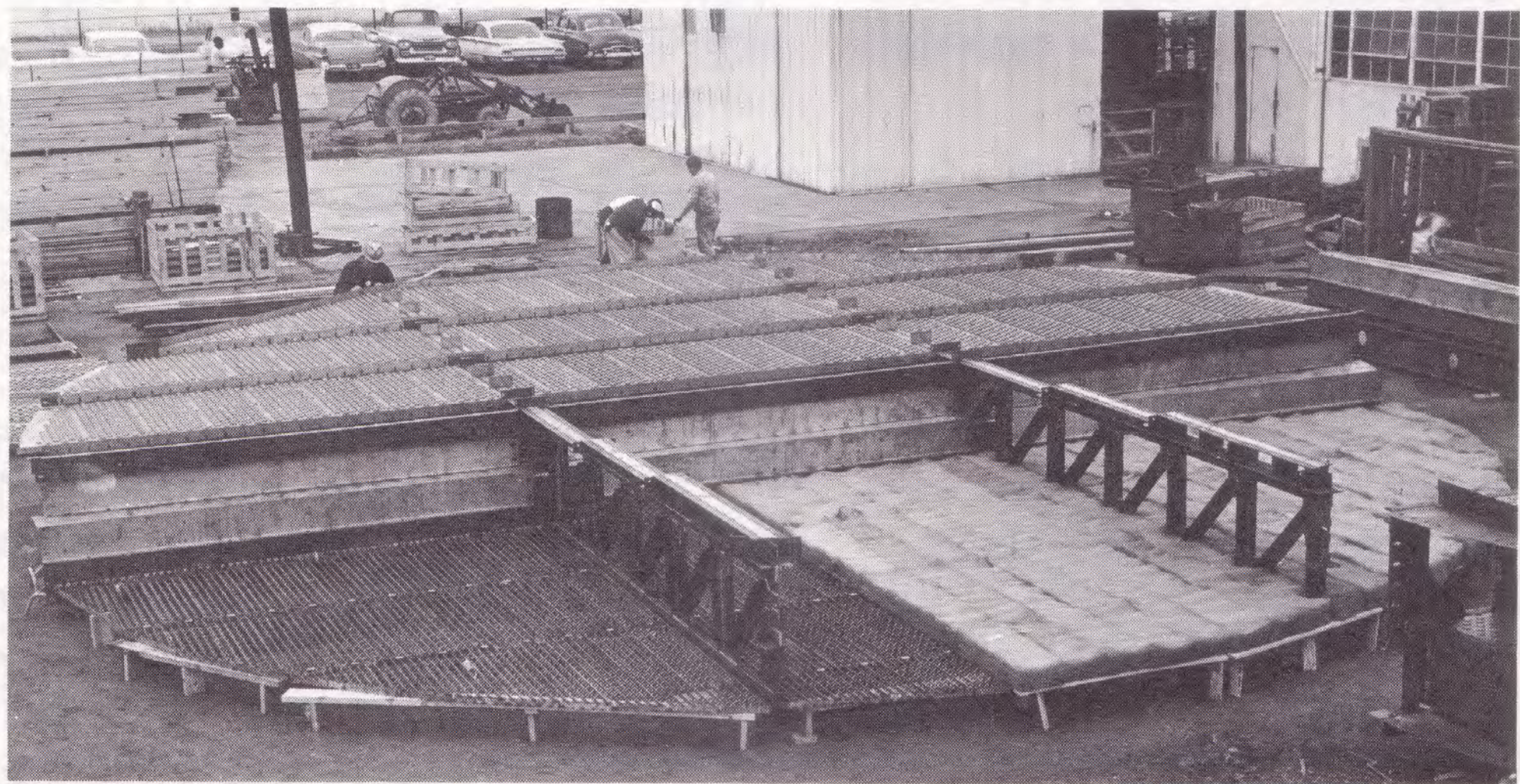








C





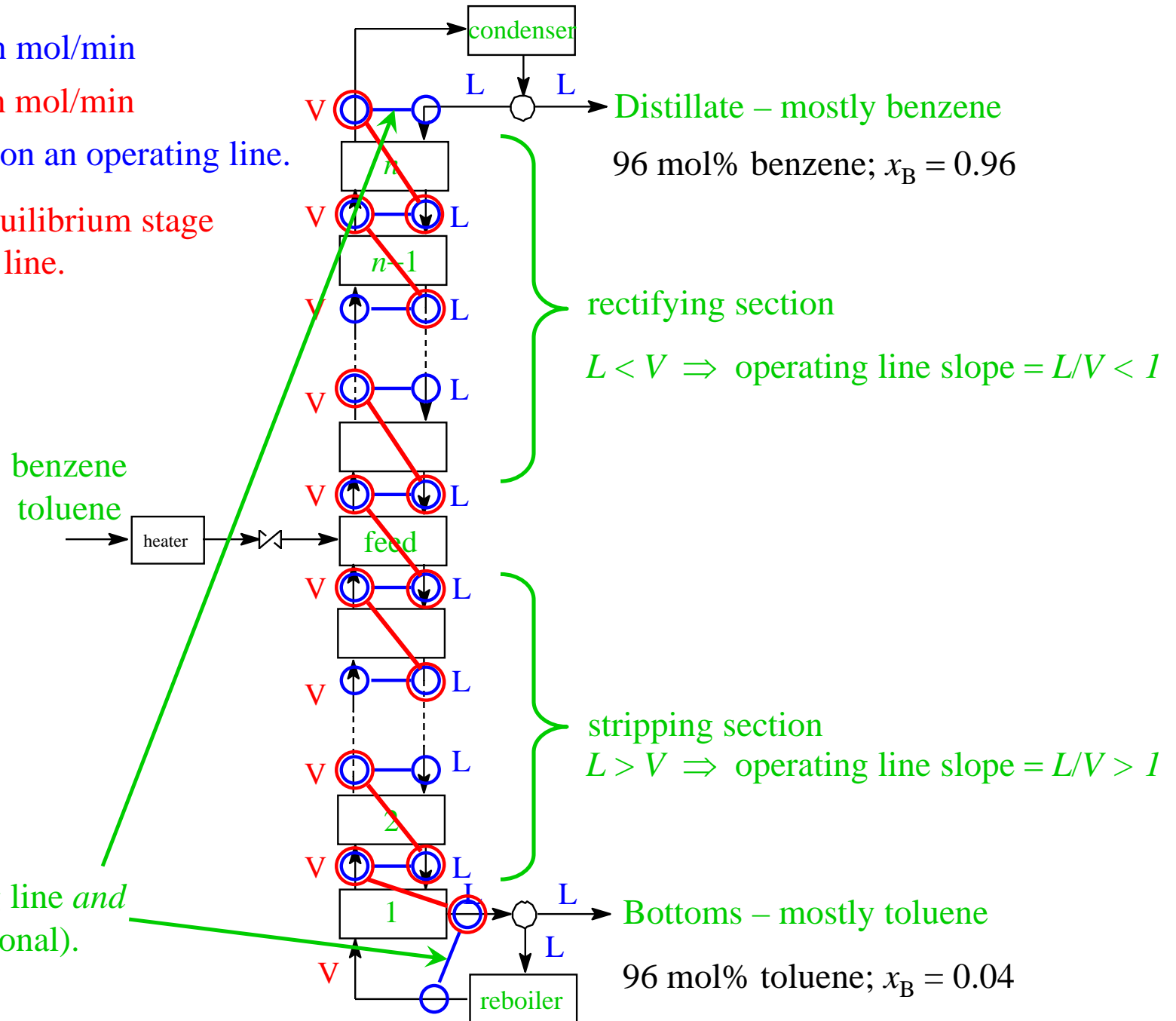
A Distillation Column

$L \equiv$ liquid flow rate, in mol/min

$V \equiv$ vapor flow rate, in mol/min

Adjacent x - y pairs are on an operating line.

x - y pairs leaving an equilibrium stage are on the equilibrium line.



x - y pair on operating line *and* on $x=y$ line (the diagonal).

A Graphical Model of a Distillation Column

vapor-liquid diagram
for benzene+toluene
mixtures at 1 atm

mol fraction
benzene
in vapor

pure
toluene

plotting pair
at bottom
of column

mol fraction benzene in liquid

pure
benzene

plotting pair
at top
of column

$x=y$ diagonal

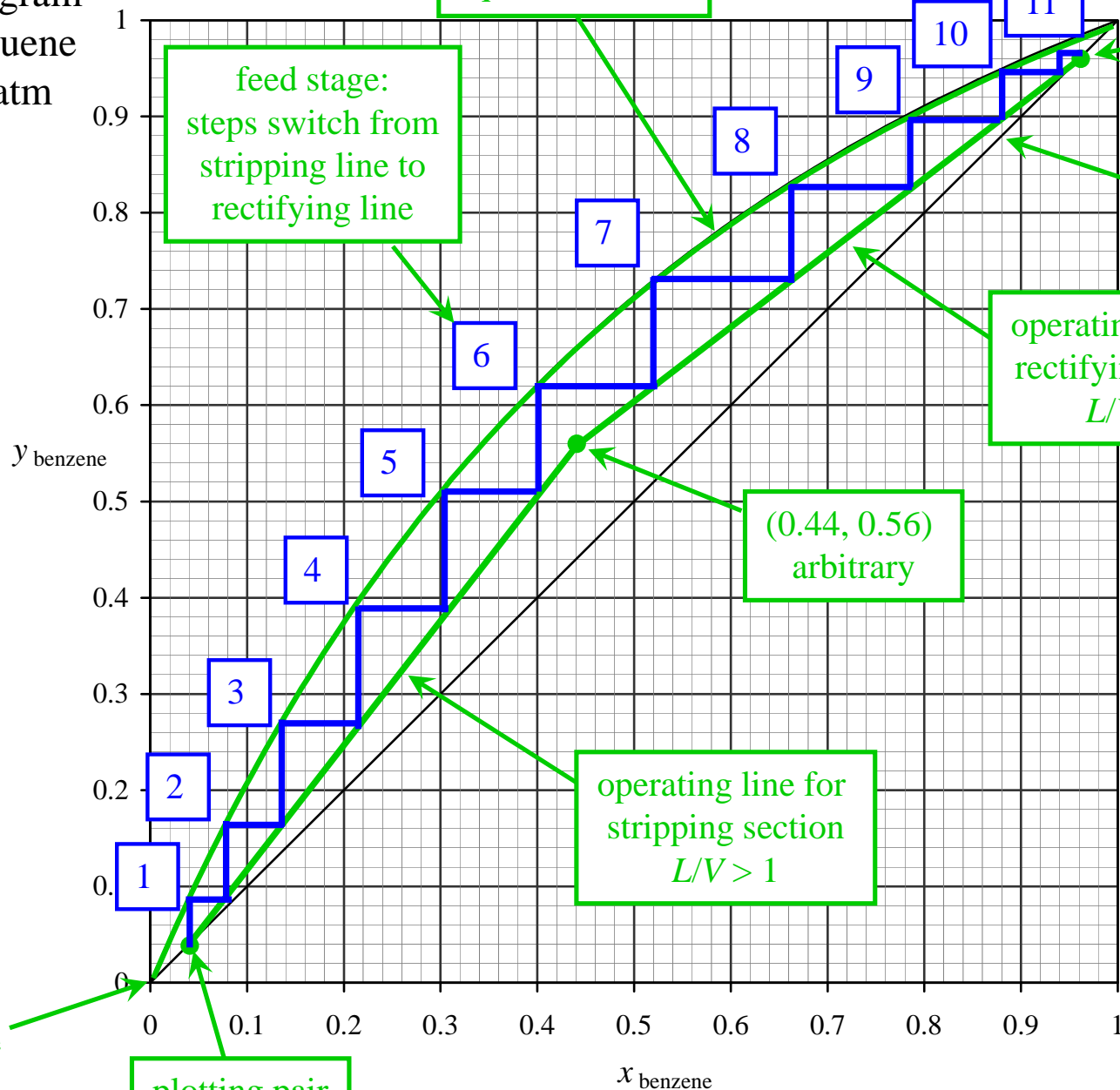
operating line for
rectifying section
 $L/V < 1$

(0.44, 0.56)
arbitrary

operating line for
stripping section
 $L/V > 1$

feed stage:
steps switch from
stripping line to
rectifying line

equilibrium line

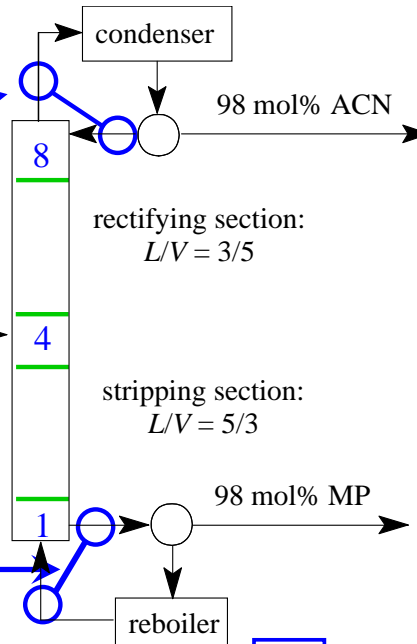


Distillation Example 2

x - y pair on operating line and
on $x=y$ line: $x = y = 0.98$

40. mol% ACN
60. mol% MP
20°C
100. mol/min

heater
 $T = ?$



$$\text{slope} = \frac{\text{rise}}{\text{run}} = \frac{3}{5} \times \frac{0.10}{0.10} = \frac{0.30}{0.50}$$

$$x: 0.98 - 0.50 = 0.48$$

$$y: 0.98 - 0.30 = 0.68$$

$$\text{slope} = \frac{\text{rise}}{\text{run}} = \frac{5}{3} \times \frac{0.10}{0.10} = \frac{0.50}{0.30}$$

$$x: 0.02 + 0.30 = 0.32$$

$$y: 0.02 + 0.50 = 0.52$$

x - y pair on operating line and
on $x=y$ line: $x = y = 0.02$

equilibrium line

feed stage

y_{ACN}

pure MP

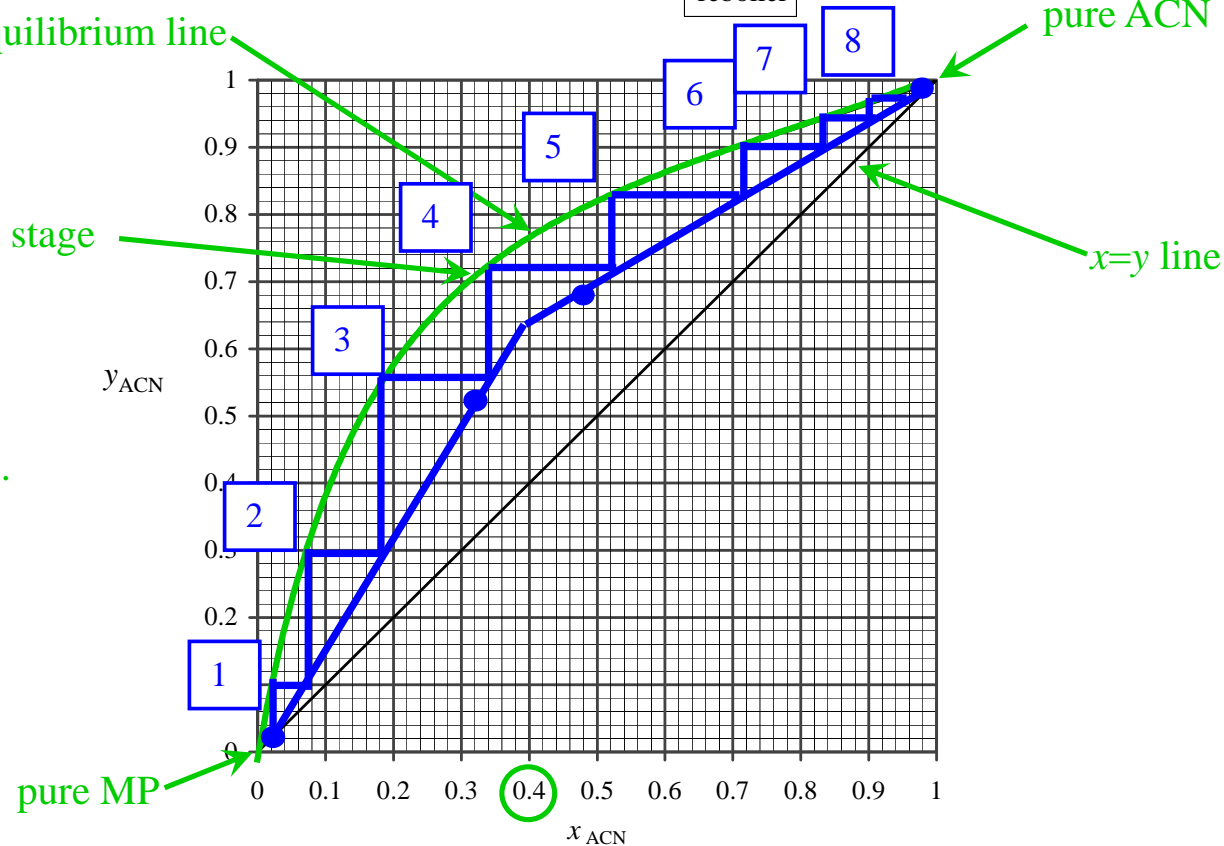
x_{ACN}

pure ACN

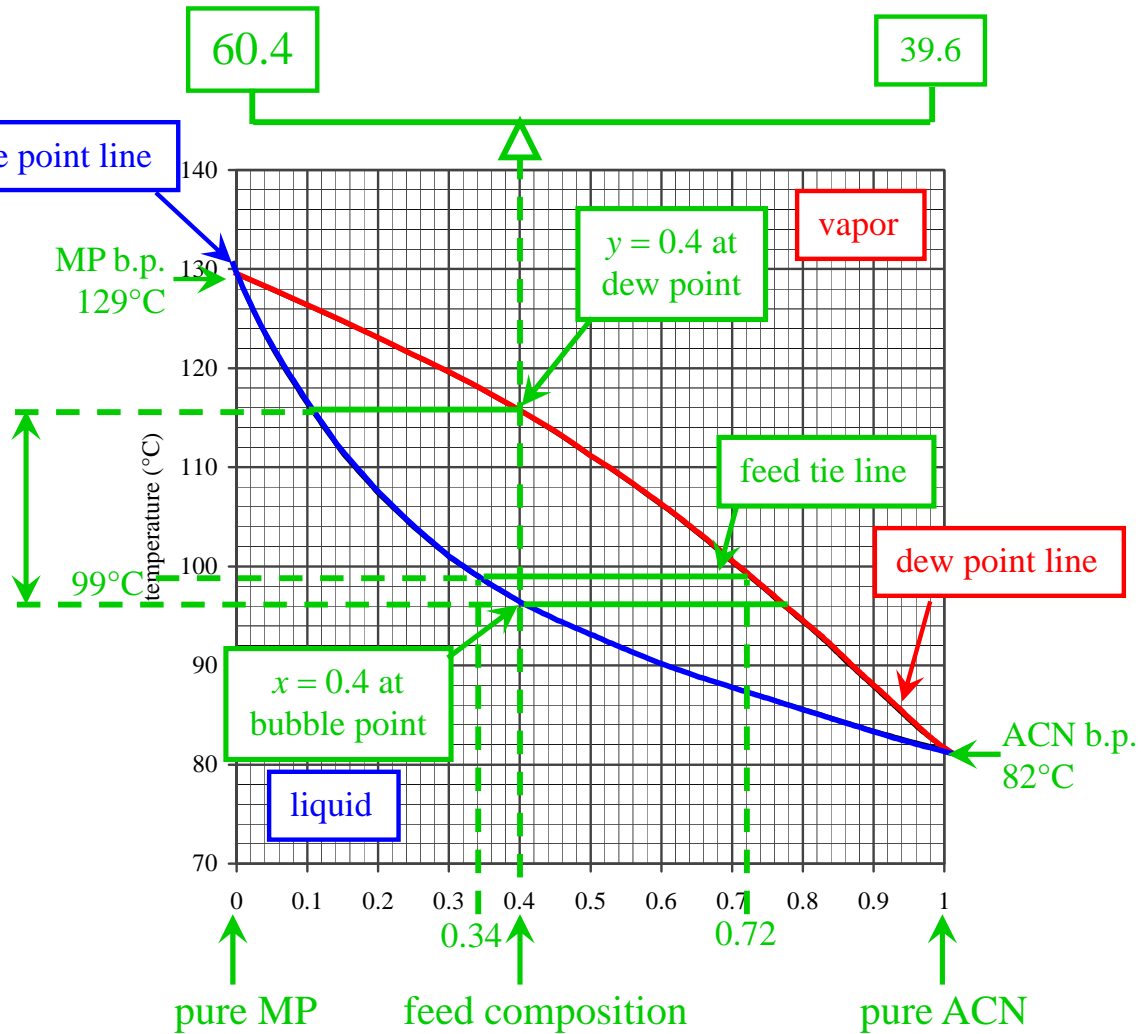
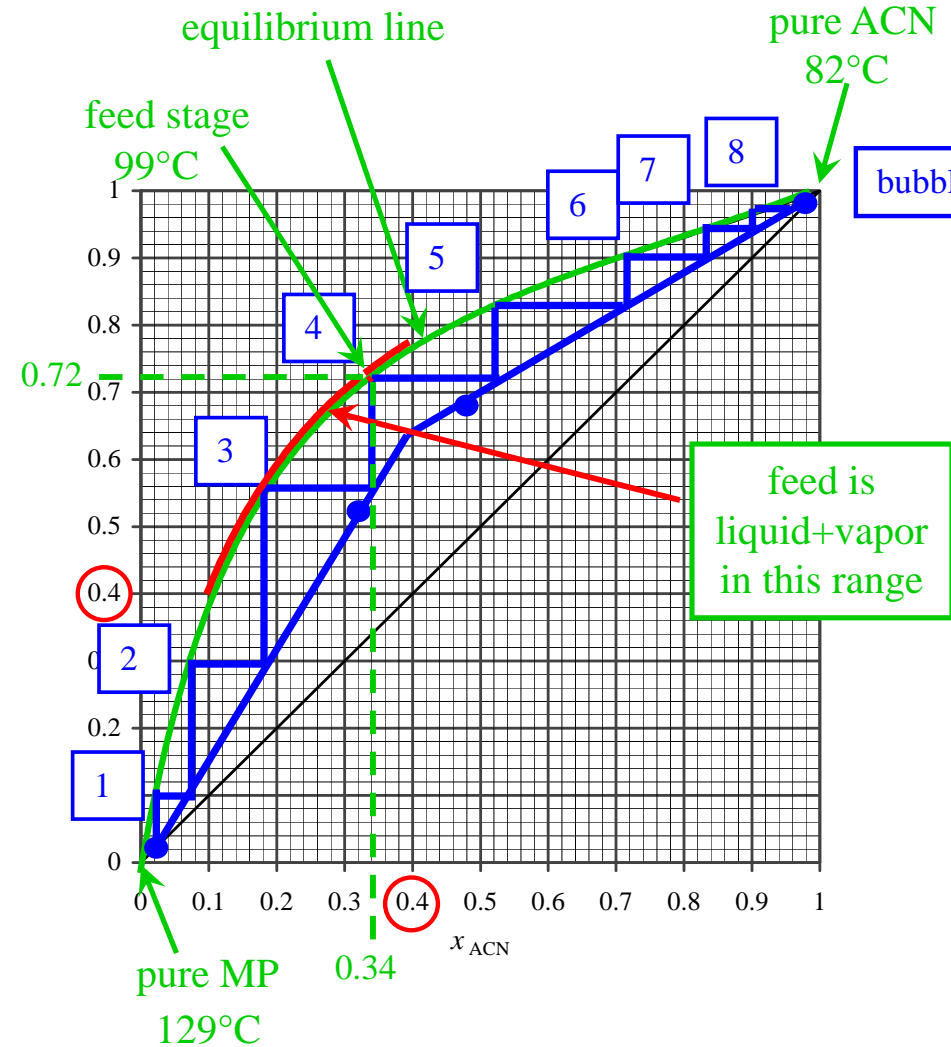
$x=y$ line

Temperature of feed?

We need a different map ...



Distillation Example 2, continued.



liquid+vapor everywhere
 Equilibrium on one line only
 Need two streams to plot a point
 Use operating lines

liquid+vapor in one region only
 Equilibrium everywhere
 One stream defines a point
 Use tie lines

Distillation Example 2

x - y pair on operating line and
on $x=y$ line: $x = y = 0.98$

40. mol% ACN
60. mol% MP
20°C
100. mol/min

heater
 $T = ?$

x - y pair on operating line and
on $x=y$ line: $x = y = 0.02$

$V = 100$

condenser

$L = 40$

$L = 60$

rectifying section:
 $L/V = 3/5$

stripping section:
 $L/V = 5/3$

$L = 150$ $L = 60$

$L = 90$

reboiler

$V = 90$

$$\text{slope} = \frac{\text{rise}}{\text{run}} = \frac{3}{5} \times \frac{0.10}{0.10} = \frac{0.30}{0.50}$$

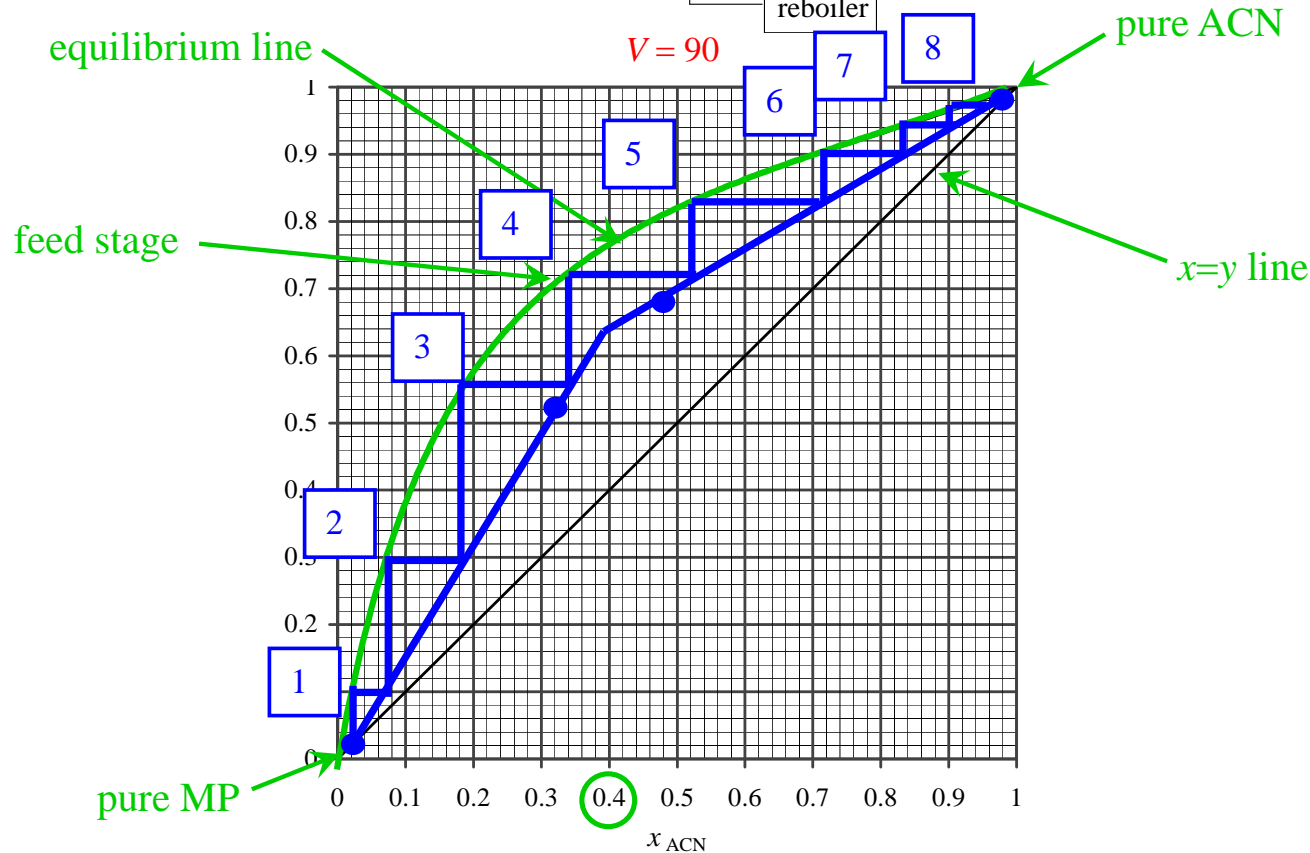
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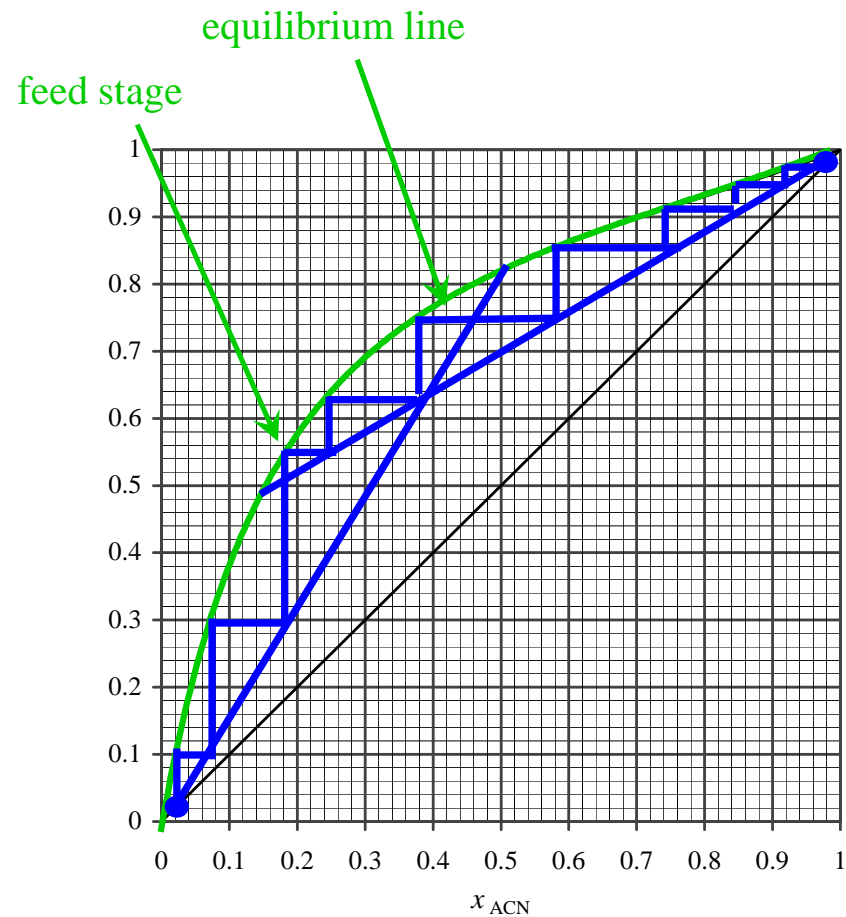
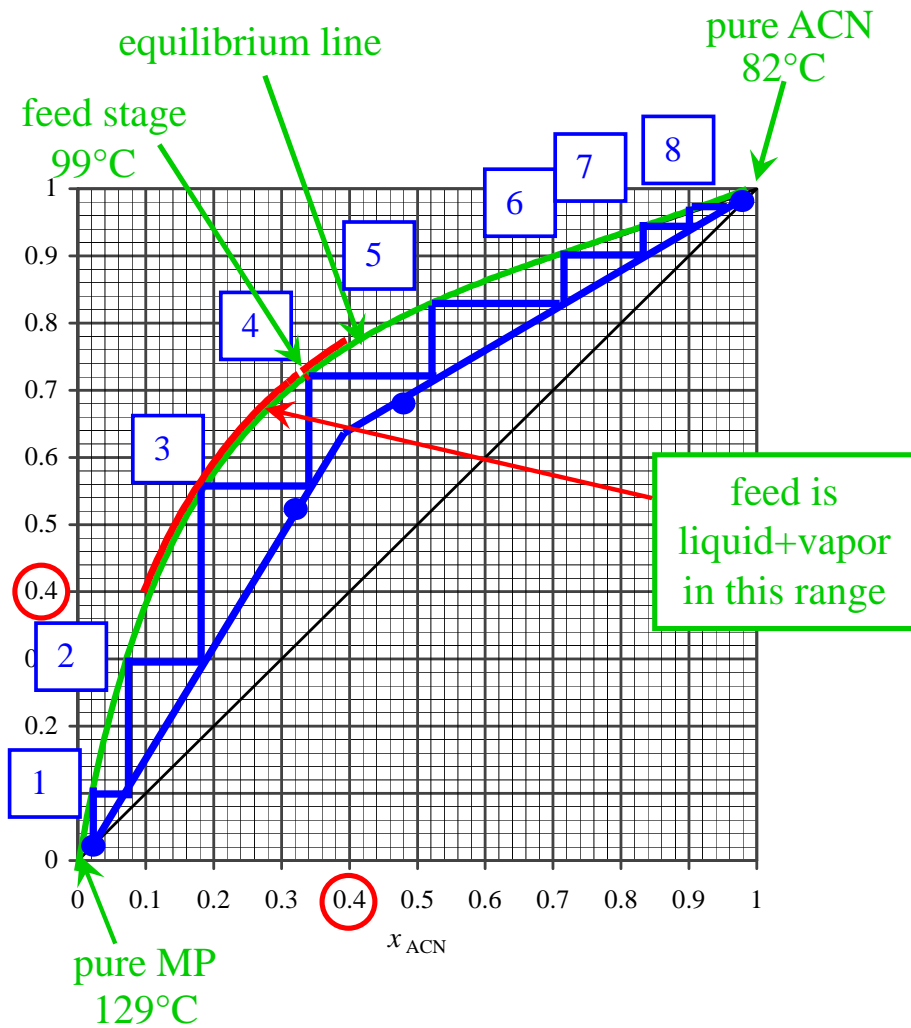
$$\text{slope} = \frac{\text{rise}}{\text{run}} = \frac{5}{3} \times \frac{0.10}{0.10} = \frac{0.50}{0.30}$$

$$x: 0.02 + 0.30 = 0.32$$

$$y: 0.02 + 0.50 = 0.52$$



Distillation Example 2, continued.

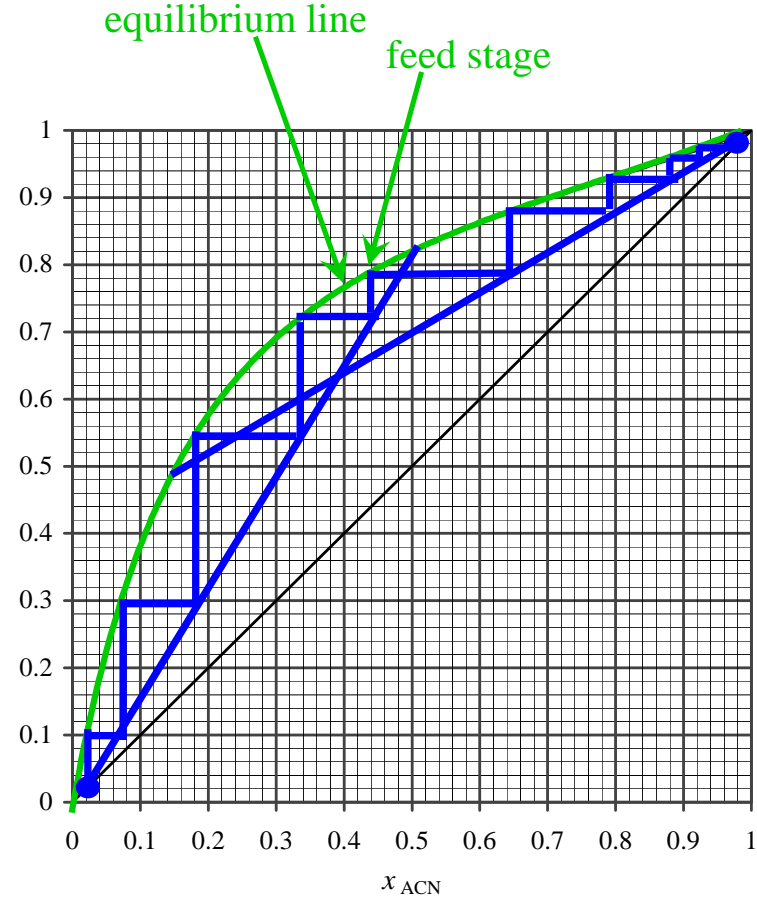
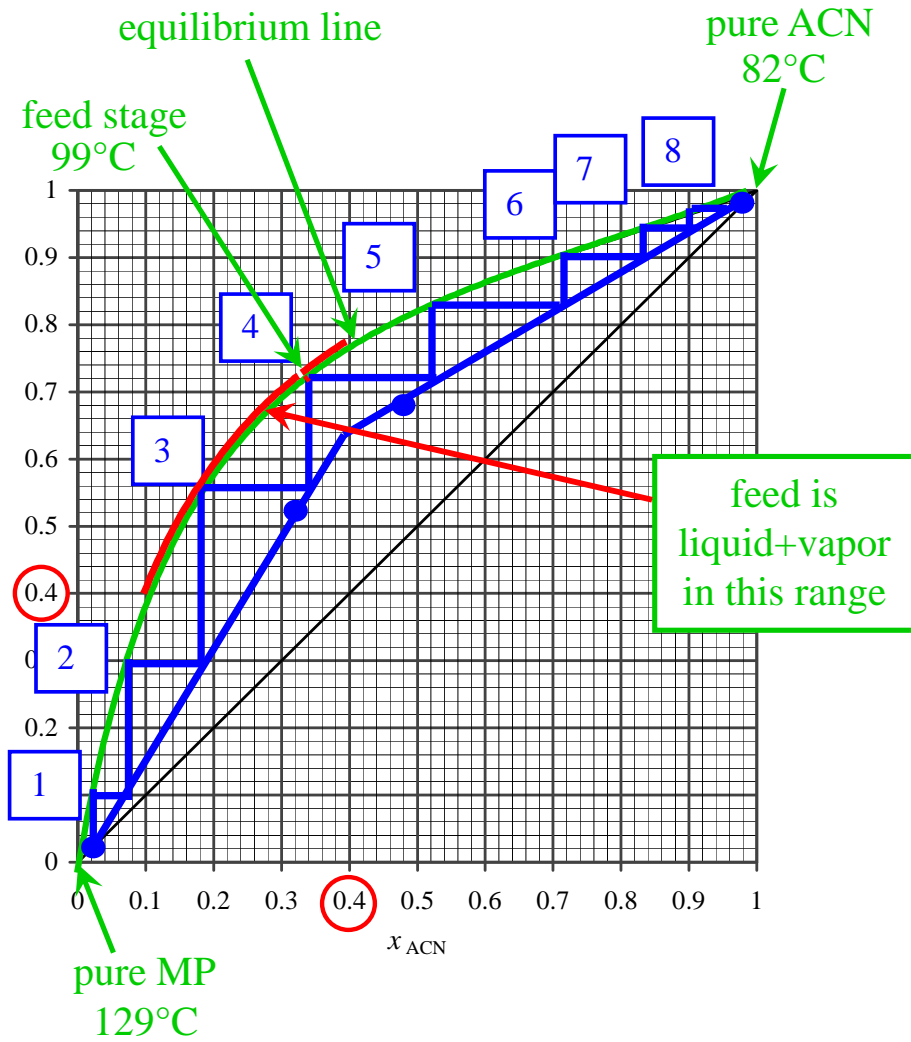


Same operating lines

Valid construction? Valid operation?

Valid!

Distillation Example 2, continued.



Same operating lines

Valid construction? Valid operation?

Not Valid!

Prelim 2 2025 Statistics

Mean: 90 / 120 (75%)

Std. Deviation: 20

A - K: Kong (Front of room)

L - Z: Angel (Back of room)

Solution is posted.

Problem 1: $22 \pm 8 / 35$ (62%)

Problem 2: $18 \pm 3 / 20$ (90%)

Problem 3: $13 \pm 6 / 20$ (69%)

Problem 4: $15 \pm 5 / 20$ (77%)

Problem 5: $20 \pm 7 / 25$ (78%)